

Highly ambitious outlines for Physics 211ABC sequence

SOLID STATE PHYSICS

211A (this will be offered as section C of 239 during F19)

1. Phases of matter
 - a. the mother of all Hamiltonians (H)
 - b. classical and quantum phase transitions

2. Spontaneous symmetry breaking
 - a. Landau theory
 - b. generalized rigidity
 - c. lower critical dimension
 - d. Goldstone and Hohenberg-Mermin-Wagner theorems

3. Crystals
 - a. crystallography
 - b. Landau theory of weak crystallization
 - c. phonons: dispersion, Debye-Waller factor, $S(\mathbf{q},\omega)$
 - d. elasticity
 - e. exotica: quasicrystals, defects

4. Metals and insulators
 - a. electrons in a periodic potential generated by SSB (Bloch's thm and consequences)
 - b. band gaps; metals and insulators in the simple band picture of solids
 - c. semiconductors and band insulators
 - d. thermodynamic consequences: Pauli susceptibility, heat capacity, compressibility
 - e. Boltzmann transport theory
 - f. Hartree-Fock and density functional theory
 - g. screening, RPA, Lindhard function, $S(\mathbf{q},\omega)$
 - h. linear response and optical properties
 - i. interactions can change the picture: Hubbard model, Mott insulators

5. Mesosocopia and localization
 - a. Landauer formula and its multichannel generalization; Pichard's formula
 - b. Interference effects; universal conductance fluctuations
 - c. weak localization
 - d. Anderson localization: localized vs. extended states, models of disorder, scaling theory

211B

1. Fermi liquid theory
 - a. adiabatic continuity
 - b. free energy as a functional of distribution $n(\mathbf{k}\sigma)$; interactions $f(\mathbf{k}\sigma, \mathbf{k}'\sigma')$
 - c. quasiparticles
 - d. equilibrium properties and thermodynamic stability
 - e. Landau-Boltzmann equation

2. Second quantization
 - a. Green's functions for fermionic systems
 - b. diagrammatic perturbation theory
 - c. theory of the electron gas

3. Instabilities of the Fermi liquid : mean field theory and gap equation
 - a. charge density wave
 - b. spin density wave
 - c. superconductivity
 - d. exciton condensate

4. Superconductivity
 - a. Ginzburg-Landau theory
 - b. effective attraction mediated by phonons
 - c. BCS theory
 - d. electromagnetic response for BCS superconductors
 - e. Josephson effect and Josephson junctions
 - f. vortices and duality; KT transition

5. Quantum magnetism of insulators
 - a. Heisenberg model; superexchange
 - b. spin wave theory and Schwinger boson formulation
 - c. quantum disordered states below the LCD; Néel vs. VBS vs. spin liquid states
 - d. spin chains: Bethe Ansatz ($S=1/2$), Haldane gap and VBS ($S=1$), continuum field theory

211C

1. Interacting bosonic systems

- a. Bose-Hubbard model
- b. mean field analysis: superfluidity and Mott lobes; the Mott-SF transition
- c. superfluids, Gross-Pitaevskii model (NLSE)
- d. vortices

2. Kondo effect and heavy fermion liquids

- a. single impurity Kondo effect, mean field approach, poor man's scaling
- b. two channel Kondo problem
- c. Kondo lattice Hamiltonian and its phases (heavy fermion metal, Kondo insulator)

3. Bosonization and Luttinger liquid theory

- a. 1D interacting Fermi systems, "g"-ology
- b. abelian bosonization and the Luttinger model
- c. spin-charge separation
- d. sine-Gordon theory, Coulomb gas description
- e. KT transition and RG, spin and charge gaps

4. Quantum Hall effect

- a. Landau levels for ballistic and Dirac dispersions
- b. lowest Landau level plus disorder: the integer quantum Hall effect
- c. TKNN formula and Chern numbers
- d. Laughlin's wavefunctions (abelian case); quasiparticles (charge, statistics), Chern insulators
- e. Hierarchy of abelian FQH states; composite fermions
- f. CSGL theory of the FQHE (K-matrices)
- g. exotica: skyrmions, half-filled LL, nonabelions, QH ferromagnetism

5. Quantum spin liquids

- a. confinement / deconfinement (Fradkin-Shenker)
- b. Kitaev's toric code and honeycomb lattice models
- c. long-ranged entanglement
- d. spin ice and quantum spin ice
- e. emergent gauge theories