

# Final Projects

project 1 Consider the harmonic oscillator

$$L = \frac{1}{2} m \dot{x}^2 - \frac{1}{2} m \omega^2 x^2$$

- (a) Evaluate the ground state energy  $E_0$  in Monte Carlo path integral
- (b) Plot the ground state probability distribution and compare with the expected analytic form
- (c) Evaluate the energy  $E_1$  of the first excited state. Can you detect a change in the electron probability distribution?
- (d) Calculate  $\langle E(\theta) \rangle$  at finite temperature  $\theta$  and compare with the expected analytic form as a function of temperature  $\theta$ . Find the classical and quantum regime

project 2 Anharmonic double well potential

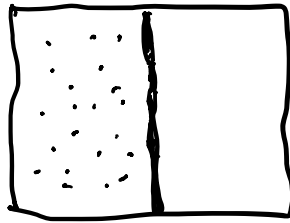
$$L = \frac{1}{2} m \dot{x}^2 - a (x^2 - b^2)^2$$

- (a) Evaluate the ground state energy  $E_0$  in Monte Carlo path integral and the first excited state  $E_1$
- (b) Plot the ground state probability distribution
- (c) Plot  $E_1 - E_0$  as a function of the barrier height

project 3 2 dimensional harmonic oscillator with 4 arts  
(a) - (d) like in project 1

project 4

ideal gas in box with  
wall partition removed  
2 dim



$$pV = RT$$

project 5

2 dim Ising model

calculate the specific heat  
as a function of temperature