

$$\begin{aligned}
 3-5. \quad (a) \quad R &= \frac{mu}{qB} = \frac{[(2E_k/e)(e/m)]^{1/2}}{(e/m)(B)} \\
 &= \frac{1}{B} \sqrt{\frac{2E_k/e}{e/m}} = \frac{1}{0.325T} \left[\frac{(2)(4.5 \times 10^4 \text{ eV}/e)}{1.76 \times 10^{11} \text{ kg}} \right]^{1/2} = 2.2 \times 10^{-3} \text{ m} = 2.2 \text{ mm}
 \end{aligned}$$

$$\begin{aligned}
 (b) \quad \text{frequency} \quad f &= \frac{u}{2\pi R} = \frac{\sqrt{(2E_k/e)(e/m)}}{2\pi R} \\
 &= \frac{[(2)(4.5 \times 10^4 \text{ eV}/e)(1.76 \times 10^{11} \text{ C/kg})]^{1/2}}{2\pi(2.2 \times 10^{-3} \text{ m})} = 9.1 \times 10^9 \text{ Hz}
 \end{aligned}$$

$$\text{period} \quad T = 1/f = 1.1 \times 10^{-10} \text{ s}$$

$$\begin{aligned}
 3-6. \quad (a) \quad 1/2mu^2 = E_k, \text{ so } u &= \sqrt{(2E_k/e)(e/m)} \\
 \therefore u &= [(2)(2000 \text{ eV}/e)(1.76 \times 10^{11} \text{ C/kg})]^{1/2} = 2.65 \times 10^7 \text{ m/s}
 \end{aligned}$$

$$(b) \quad \Delta t_1 = \frac{x_1}{u} = \frac{0.05 \text{ m}}{2.65 \times 10^7 \text{ m/s}} = 1.89 \times 10^{-9} \text{ s} = 1.89 \text{ ns}$$

$$(c) \quad mu_y = F \Delta t_1 = e \mathcal{E} \Delta t_1$$

$$\therefore u_y = (e/m) \mathcal{E} \Delta t_1 = (1.76 \times 10^{11} \text{ C/kg}) (3.33 \times 10^3 \text{ V/m}) (1.89 \times 10^{-9} \text{ s}) = 1.11 \times 10^6 \text{ m/s}$$

3-24. Photon energy $E = hf = hc / \lambda$

(a) For $\lambda = 380nm$: $E = (1240eV \cdot nm) / 380nm = 3.26eV$

For $\lambda = 750nm$: $E = (1240eV \cdot nm) / 750nm = 1.65eV$

(b) $E = hf = (4.14 \times 10^{-15} eV \cdot s)(100 \times 10^6 s^{-1}) = 4.14 \times 10^{-7} eV$

$$3-26. \quad (a) \quad \lambda_i = \frac{hc}{\phi} = \frac{1240eV \cdot nm}{1.9eV} = 653nm, \quad f_i = \frac{\phi}{h} = \frac{1.9eV}{4.136 \times 10^{-15} eV \cdot s} = 4.59 \times 10^4 Hz$$

$$(b) \quad V_0 = \frac{1}{e} \left(\frac{hc}{\lambda} - \phi \right) = \frac{1}{e} \left(\frac{1240eV \cdot nm}{300nm} - 1.9eV \right) = 2.23V$$

$$(c) \quad V_0 = \frac{1}{e} \left(\frac{hc}{\lambda} - \phi \right) = \frac{1}{e} \left(\frac{1240eV \cdot nm}{400nm} - 1.9eV \right) = 1.20V$$

$$3-27. \quad (a) \quad \text{Choose } \lambda = 550nm \text{ for visible light. } nhf = E \rightarrow \frac{dn}{dt} hf = \frac{dE}{dt} = P$$

$$\frac{dn}{dt} = \frac{P}{hf} = \frac{P\lambda}{hc} = \frac{(0.05 \times 100W)(550 \times 10^{-9}m)}{(6.63 \times 10^{-34} J \cdot s)(3.00 \times 10^8 m/s)} = 1.38 \times 10^{19} / s$$

$$(b) \quad flux = \frac{\text{number radiated} / \text{unit time}}{\text{area of the sphere}} = \frac{1.38 \times 10^{19} / s}{4\pi(2m)^2} = 2.75 \times 10^{17} / m^2 \cdot s$$

$$3-28. \quad (a) \quad hf = \phi \quad \therefore \quad f_t = \frac{\phi}{h} = \frac{4.22eV}{4.14 \times 10^{-15} eV \cdot s} = 1.02 \times 10^{15} \text{ Hz}$$

$$(b) \quad f = c/\lambda = \frac{3.00 \times 10^8 \text{ m/s}}{560 \times 10^{-9} \text{ m}} = 5.36 \times 10^{14} \text{ Hz} \quad \text{No.}$$

$$\text{Available energy/photon } hf = (4.14 \times 10^{-15} eV \cdot s)(5.36 \times 10^{14} \text{ Hz}) = 2.22eV.$$

This is less than ϕ .

$$3-31. \quad E = n \frac{hc}{\lambda} = \frac{(60)(6.63 \times 10^{-34} \text{ J}\cdot\text{s})(3.00 \times 10^8 \text{ m/s})}{550 \times 10^{-9} \text{ m}} = 2.17 \times 10^{-17} \text{ J}$$

$$3-32. \quad (\text{a}) \quad \phi = \frac{hc}{\lambda} = \frac{1240 \text{ eV}\cdot\text{nm}}{653 \text{ nm}} = 1.90 \text{ eV}$$

$$(\text{b}) \quad E_k = \frac{hc}{\lambda} - \phi = \frac{1240 \text{ eV}\cdot\text{nm}}{300 \text{ nm}} - 1.90 \text{ eV} = 2.23 \text{ eV}$$

3-34. Equation 3-24: $\lambda_m = \frac{1.24 \times 10^3}{V} \text{ nm} = \frac{1.24 \times 10^3}{80 \times 10^3 \text{ V}} = 0.016 \text{ nm}$

$$3-36. \quad \lambda_2 - \lambda_1 = \frac{h}{mc}(1 - \cos \theta) = \frac{(6.63 \times 10^{-34} \text{ J}\cdot\text{s})(1 - \cos 110^\circ)}{(9.11 \times 10^{-31} \text{ kg})(3.00 \times 10^8 \text{ m/s})} = 3.26 \times 10^{-12} \text{ m}$$

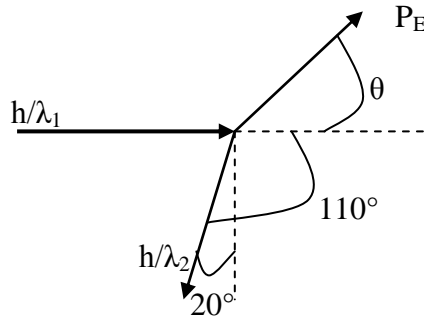
$$\lambda_1 = \frac{hc}{E_1} = \frac{(6.63 \times 10^{-34} \text{ J}\cdot\text{s})(3 \times 10^8 \text{ m/s})}{(0.511 \times 10^6 \text{ eV})(1.60 \times 10^{-19} \text{ J/eV})} = 2.43 \times 10^{-12} \text{ m}$$

$$\lambda_2 = \lambda_1 + 3.26 \times 10^{-12} \text{ m} = (2.43 + 3.26) \times 10^{-12} \text{ m} = 5.69 \times 10^{-12} \text{ m}$$

$$E_2 = \frac{hc}{\lambda_2} = \frac{1240eV \cdot nm}{5.69 \times 10^{-3} nm} = 2.18 \times 10^5 eV = 0.218 MeV$$

Electron recoil energy $E_e = E_1 - E_2$ (Conservation of energy)

$E_e = 0.511 MeV - 0.218 MeV = 0.293 MeV$. The recoil electron momentum makes an angle θ with the direction of the initial photon.



$$\frac{h}{\lambda_2} \cos 20^\circ = p_e \sin \theta = (1/c) \sqrt{E^2 - (mc^2)^2} \sin \theta \quad (\text{Conservation of momentum})$$

$$\sin \theta = \frac{(3.00 \times 10^8 m/s)(6.63 \times 10^{-34} J \cdot s) \cos 20^\circ}{(5.69 \times 10^{-12} m) \left[(0.804 MeV)^2 - (0.511 MeV)^2 \right]^{1/2} (1.60 \times 10^{-13} J / MeV)}$$

$$= 0.330 \text{ or } \theta = 19.3^\circ$$

3-38. $\Delta\lambda = \lambda_2 - \lambda_1 = \Delta\lambda = \frac{h}{mc}(1 - \cos\theta) = 0.01\lambda_1$ Equation 3-25

$$\lambda_1 = (100) \frac{h}{mc} (1 - \cos\theta) = (100)(0.00243\text{nm})(1 - \cos 90^\circ) = 0.243\text{nm}$$

3-39. (a) $E_1 = \frac{hc}{\lambda_1} = \frac{1240\text{eV}\cdot\text{nm}}{0.0711\text{nm}} = 1.747 \times 10^4 \text{eV}$

(b) $\lambda_2 = \lambda_1 + \frac{h}{mc}(1 - \cos\theta) = 0.0711\text{nm} + (0.00243\text{nm})(1 - \cos 180^\circ) = 0.0760\text{nm}$

(c) $E_2 = \frac{hc}{\lambda_2} = \frac{1240\text{eV}\cdot\text{nm}}{0.0760\text{nm}} = 1.634 \times 10^4 \text{eV}$

(d) $E_e = E_1 - E_2 = 1.128 \times 10^3 \text{eV}$

3-42. (a) Compton wavelength = $\frac{h}{mc}$

electron: $\frac{h}{mc} = \frac{6.63 \times 10^{-34} \text{ J}\cdot\text{s}}{(9.11 \times 10^{-31} \text{ kg})(3.00 \times 10^8 \text{ m/s})} = 2.43 \times 10^{-12} \text{ m} = 0.00243 \text{ nm}$

proton: $\frac{h}{mc} = \frac{6.63 \times 10^{-34} \text{ J}\cdot\text{s}}{(1.67 \times 10^{-27} \text{ kg})(3.00 \times 10^8 \text{ m/s})} = 1.32 \times 10^{-15} \text{ m} = 1.32 \text{ fm}$

(b) $E = \frac{hc}{\lambda}$

(i) electron: $E = \frac{1240 \text{ eV}\cdot\text{nm}}{0.00243 \text{ nm}} = 5.10 \times 10^5 \text{ eV} = 0.510 \text{ MeV}$

(ii) proton: $E = \frac{1240 \text{ eV}\cdot\text{nm}}{1.32 \times 10^{-6} \text{ nm}} = 9.39 \times 10^8 \text{ eV} = 939 \text{ MeV}$