

**PHYSICS 239 : SUPERCONDUCTIVITY**  
**HW ASSIGNMENT #4**

**(1)** Calculate the zero temperature tunneling density of states  $N(\omega)$  in  $d$ -wave nodal superconductors. You need to go through the steps to express  $N(\omega)$  in term of elliptic integrals (complete, first kind). Please derive the asymptotic behavior for  $\hbar\omega/\Delta \rightarrow 0, 1,$  and  $\infty,$  respectively. Compare your results with those of the  $s$ -wave superconductors. (See pages 11-12 in the lecture notes, chapter 5.)

**(2)** Calculate the low temperature paramagnetic magnetic susceptibility (NMR Knight shift) of  $d$ -wave nodal superconductors at  $k_B T \ll \Delta$ . The numeric coefficient is unimportant, but the power of the temperature dependence is important. You can compare your result with that of the  $s$ -wave case. You also need to learn the Yoshida function, which is a very useful function for thermodynamics of superconductors. Can you anticipate your results directly from the density of states of nodal quasi-particles? (See pages 16-17 in the lecture notes, chapter 5.)

**(2)** Explain the physical meaning of the  $d$ -vector,  $d(\mathbf{k})$ ? How does one use the  $d$ -vector to describe the triplet Cooper pairing?