

Problem Set VI: Due Monday, December 2, 2013

- 1.) FW 4.16
- 2.) FW 4.6, a.) - c.)
- 3.) FW 7.1, a, b. You need only discuss d' Alembert solution in B.
- 4.) Consider a string of length L and mass-per-length μ which is, as usual, clamped at both ends. Assume the tension is T .

Express the Hamiltonian density in terms of the Fourier coefficients, thereby converting the problem to one of particle dynamics. (Hint: Expand the displacement in terms of the *spatial* eigenfunctions.) Derive the Hamiltonian EOMs.

- 5a.) Generalize the derivation of the nonlinear wave equation for a string to that for a 2D membrane (i.e. drum head), with clamped boundary. Show that you recover the wave equation in the linear limit.
- 5b.) Derive the energy-momentum conservation equations for linear waves on this membrane.