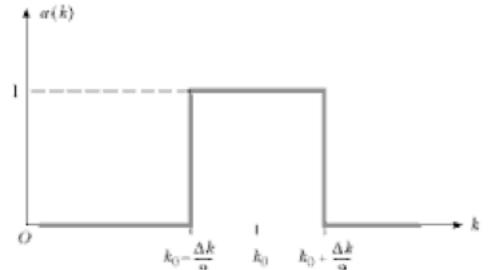
(a) Show that the matter wave packet whose amplitude distribution a(k) is a rectangular pulse of height unity, width Δk , and centered at k_0 has the form $f(x) = \frac{\Delta k}{\sqrt{2\pi}} \frac{\sin(\Delta k \cdot x/2)}{(\Delta k \cdot x/2)} e^{ik_0 x}$



A simple amplitude distribution specifying a uniform contribution of all wavenumbers from $k_0 = \Delta k/2$ to $k_0 + \Delta k/2$. Although we have used only positive k's here, both positive and negative k values are allowed, in general corresponding to waves traveling to the right (k > 0) or left (k < 0).