

21.1 The charge is

$$\Delta Q = I \times \Delta t = 30 \times 10^{-6} A \times 40s = 1.2 \times 10^{-3} C.$$

So the number of electrons is:

$$\frac{Q}{e} = \frac{1.2 \times 10^{-3} C}{1.6 \times 10^{-19} C} = 7.5 \times 10^{15}.$$

21.5 From the periodic table of the elements, we can find the molar mass of aluminum is 27g/mol, which means the mass of one mole aluminum atoms is 27g. We also know that one mole of any substance contains Avogadro's number ( $6.02 \times 10^{23}/mol$ ) of atoms, so the mass of each aluminum atom is:

$$\frac{27g/mol}{6.02 \times 10^{23}/mol} = 4.5 \times 10^{-23} g.$$

With the density  $2.7g/cm^3$ , now we can find the number density of aluminum atom:

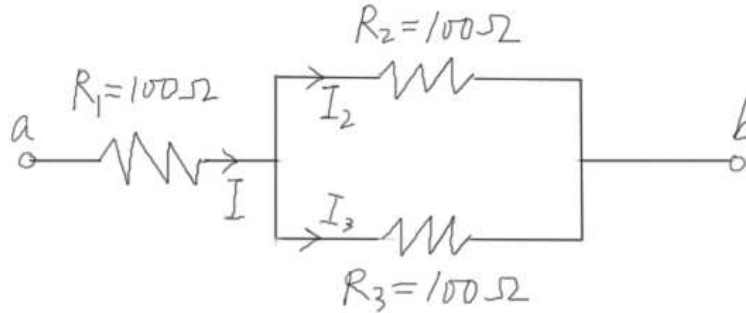
$$n = \frac{2.7g/cm^3}{4.5 \times 10^{-23}g} = 6 \times 10^{22}/cm^3 = 6 \times 10^{28}/m^3.$$

Because one conduction electron is supplied by each atom, the number density of conduction electron equals the number density of aluminum atom. So from  $I = nqv_dA$ , we have:

$$v_d = \frac{I}{nqA} = \frac{5A}{6 \times 10^{28}/m^3 \times 1.6 \times 10^{-19}C \times 4 \times 10^{-6}m^2} = 1.3 \times 10^{-4}m/s$$

21.30 and 21.31 are on next page.

21.30



(a) From  $P = I^2 R$  and all three resistors have the same  $R$ , we know that the current that pass through each of them should be smaller than:

$$I = \sqrt{P/R} = \sqrt{25W/100\Omega} = 0.5A.$$

But  $I_2$  and  $I_3$  are always smaller than  $I_1$  (in this case  $I_2 = I_3 = I_1/2$ ), so the maximum voltage is obtained when  $I_1 = 0.5A$ . Assume that the equivalent resistance of  $R_2$  and  $R_3$  is  $R_{eq}$ , and they satisfy:

$$\frac{1}{R_{eq}} = \frac{1}{R_2} + \frac{1}{R_3},$$

so we can get  $R_{eq} = 50\Omega$ . So the total resistance of these three resistors is:

$$R = R_1 + R_{eq} = 100\Omega + 50\Omega = 150\Omega.$$

So the voltage between  $a$  and  $b$  is  $0.5A \times 150\Omega = 75V$ .

(b) For  $R_1$ :

$$P_1 = I_1^2 R_1 = (0.5A)^2 \times 100\Omega = 25W.$$

For  $R_2$ :

$$P_2 = I_2^2 R_2 = (0.5A/2)^2 \times 100\Omega = 6.25W.$$

For  $R_3$ :

$$P_3 = I_3^2 R_3 = (0.5A/2)^2 \times 100\Omega = 6.25W.$$

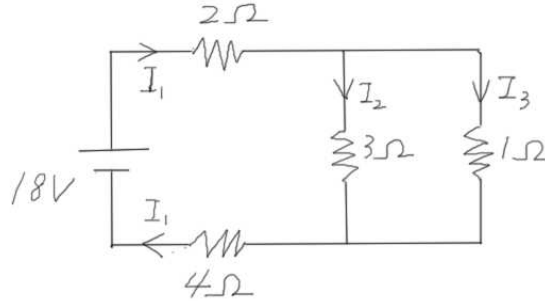
So the total power delivered is:

$$P = P_1 + P_2 + P_3 = 25W + 6.25W + 6.25W = 37.5W.$$

Another way to calculate the total power is to use the total current  $I_1$  and the total resistance  $R$ :

$$P = I_1^2 R = (0.5A)^2 \times 150\Omega = 37.5W.$$

21.31



First, assume that the equivalent resistance of  $3\Omega$  and  $1\Omega$  is  $R_{eq}$ , then they satisfy:

$$\frac{1}{R_{eq}} = \frac{1}{3\Omega} + \frac{1}{1\Omega}, \quad (1)$$

so we can get  $R_{eq} = 0.75\Omega$ . So the total resistance of these four resistors is:

$$R = 2\Omega + 0.75\Omega + 4\Omega = 6.75\Omega. \quad (2)$$

So we can get the total current  $I_1$ :

$$I_1 = \frac{18V}{6.75\Omega} = 2.67A. \quad (3)$$

Then we need to calculate  $I_2$  and  $I_3$ . First, according to conservation of charge, we have

$$I_1 = I_2 + I_3. \quad (4)$$

Then, because  $3\Omega$  and  $1\Omega$  are connected in parallel, so they have the same voltage:

$$\Delta V = 3\Omega \times I_2 = 1\Omega \times I_3. \quad (5)$$

From Eqn.(4)(5) we can get  $I_2 = 0.67A$  and  $I_3 = 2A$ .

So for  $2\Omega$ :

$$P = I_1^2 \times 2\Omega = (2.67A)^2 \times 2\Omega = 14.3W. \quad (6)$$

For  $4\Omega$ :

$$P = I_1^2 \times 4\Omega = (2.67A)^2 \times 4\Omega = 28.6W. \quad (7)$$

For  $3\Omega$ :

$$P = I_2^2 \times 3\Omega = (0.67A)^2 \times 3\Omega = 1.35W. \quad (8)$$

For  $1\Omega$ :

$$P = I_3^2 \times 1\Omega = (2A)^2 \times 1\Omega = 4W. \quad (9)$$