

9-21.  $E_{0r} = \frac{\hbar^2}{2I}$  (Equation 9-14) where  $I = \frac{1}{2}mr_0^2$  for a symmetric molecule.

$$E_{0r} = \frac{\hbar^2}{mr_0^2} = \frac{(\hbar c)^2}{mc^2 r_0^2} = \frac{(197.3 \text{ eV} \cdot \text{nm})^2}{(16 \text{ uc})^2 (931.5 \times 10^6 \text{ eV} / \text{uc}^2) (0.121 \text{ nm})^2} = 1.78 \times 10^{-4} \text{ eV}$$

9-22. For Co:  $f = 6.42 \times 10^{13} \text{ Hz}$  (See Example 9-6)

$$E_v = (v + 1/2)hf \quad (\text{Equation 9-20})$$

(a)  $E_1 - E_0 = 3hf/2 - hf/2 = hf$

$$= (4.14 \times 10^{-15} \text{ eV} \cdot \text{s}) (6.42 \times 10^{13} \text{ Hz})$$

$$= 0.27 \text{ eV}$$

(b)  $\frac{n_1}{n_0} = e^{-(E_1 - E_0)/kT}$  (from Equation 8-2)

$$0.01 = e^{-(0.27)/(8.62 \times 10^{-5})}$$

$$\ln(0.01) = -(0.27 \text{ eV}) / (8.62 \times 10^{-5} \text{ eV} / \text{K}) T$$

$$T = \frac{-(0.27 \text{ eV})}{\ln(0.01)(8.62 \times 10^{-5} \text{ eV} / \text{K})}$$

$$T = 680 \text{ K}$$

9-23. For LiH:  $f = 4.22 \times 10^{13} \text{ Hz}$  (from Table 9-7)

(a)  $E_v = (v + 1/2)hf = E_0 = hf/2 = (4.14 \times 10^{-15} \text{ eV} \cdot \text{s}) (4.22 \times 10^{13} \text{ Hz}) / 2$

$$E_0 = 0.087 \text{ eV}$$

(b)  $\mu = \frac{m_1 m_2}{m_1 + m_2}$  (Equation 9-17)

$$\mu = \frac{(7.0160 \text{ u})(1.0078 \text{ u})}{(7.0160 \text{ u}) + (1.0078 \text{ u})} = 0.8812 \text{ u}$$

(c)  $f = \frac{1}{2\pi} \sqrt{\frac{K}{\mu}}$  (Equation 9-21)

$$K = (2\pi f)^2 \mu = (2\pi)^2 (4.22 \times 10^{13} \text{ Hz})(0.8812)(1.66 \times 10^{-27} \text{ kg/u})$$

$$K = 117 \text{ N/m}$$

$$(d) E_n = n^2 h^2 / 8m r_0^2 \rightarrow r_0^2 = n^2 h^2 / 8m E_n$$

$$r_0 \approx h / (8m E_0)^{1/2}$$

$$r_0 \approx \frac{6.63 \times 10^{-34} \text{ J}\cdot\text{s}}{\left[8(0.8812u)(1.66 \times 10^{-27} \text{ kg/u})(0.087 \text{ eV})(1.60 \times 10^{-19} \text{ J/eV})\right]^{1/2}}$$

$$r_0 \approx 5.19 \times 10^{-11} \text{ m} = 0.052 \text{ nm}$$

$$9-25. (a) \mu = \frac{m_1 m_2}{m_1 + m_2} = \frac{(39.1u)(35.45u)}{39.1u + 35.45u} = 18.6u$$

$$(b) E_{0r} = \frac{\hbar^2}{2I} \quad (\text{Equation 9-14}) \quad I = \mu r_0^2$$

$$E_{0r} = \frac{\hbar^2}{2\mu r_0^2} = \frac{(\hbar c)^2}{2\mu c^2 r_0^2} \rightarrow r_0^2 = \frac{(\hbar c)^2}{2\mu c^2 E_V}$$

$$\therefore r_0 = \frac{\hbar c}{(2\mu c^2 E_V)^{1/2}} = \frac{197.3 \text{ eV}\cdot\text{nm}}{\left[2(10.6 \text{ uc}^2)(931.5 \times 10^6 \text{ eV/uc}^2)(1.43 \times 10^{-5} \text{ eV})\right]^{1/2}}$$

$$r_0 = 0.280 \text{ nm}$$

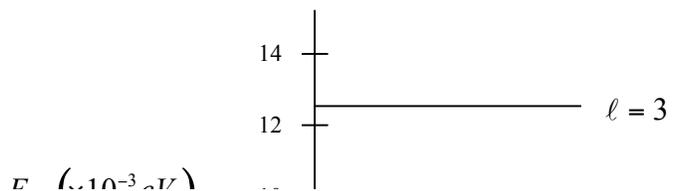
$$9-27. E_{0r} = \hbar^2 / 2I \quad \text{Treating the Br atom as fixed,}$$

$$I = m_H r_0^2 = (1.0078u)(1.66 \times 10^{-27} \text{ kg/u})(0.141 \text{ nm})^2$$

$$E_{0r} = \frac{(1.055 \times 10^{-34} \text{ J}\cdot\text{s})^2}{2(1.0078u)(1.66 \times 10^{-27} \text{ kg/u})(0.141 \text{ nm})^2 (10^{-9} \text{ m/nm})^2}$$

$$= 1.67 \times 10^{-22} \text{ J} = 1.04 \times 10^{-3} \text{ eV}$$

$$E_\ell = \ell(\ell + 1)E_{0r} \quad \text{for } \ell = 0, 1, 2, \dots \quad (\text{Equation 9-13})$$



The four lowest states have energies:

$$E_0 = 0$$

$$E_1 = 2E_{0r} = 2.08 \times 10^{-3} eV$$

$$E_2 = 6E_{0r} = 6.27 \times 10^{-3} eV$$

$$E_3 = 12E_{0r} = 12.5 \times 10^{-3} eV$$

9-29.  $E_{0r} = \frac{\hbar^2}{2I}$  where  $I = \mu r_0^2$  (Equation 9-14)

$$\text{For } K^{35}Cl: \mu = \frac{(39.102u)(34.969u)}{39.102u + 34.969u} = 18.46u$$

$$\text{For } K^{37}Cl: \mu = \frac{(39.102u)(34.966u)}{39.102u + 34.966u} = 19.00u$$

$$r_0 = 0.267nm \text{ for } KCl.$$

$$E_{0r}(K^{35}Cl) = \frac{(1.055 \times 10^{-34} J \cdot s)^2}{2(18.46u)(1.66 \times 10^{-27} kg/u)(0.267 \times 10^{-9} m)^2}$$

$$= 2.55 \times 10^{-24} J = 1.59 \times 10^{-5} eV$$

$$E_{0r}(K^{37}Cl) = \frac{(1.055 \times 10^{-34} J \cdot s)^2}{2(19.00u)(1.66 \times 10^{-27} kg/u)(0.267 \times 10^{-9} m)^2}$$

$$= 2.48 \times 10^{-24} J = 1.55 \times 10^{-5} eV$$

$$\Delta E_{0r} = 0.04 \times 10^{-5} eV$$

9-33.  $\frac{A_{21}}{B_{21}u(f)} = e^{hf/kT} - 1$  (Equation 9-42)

For the H $\alpha$  line  $\lambda=656.1\text{nm}$

$$\text{At } T = 300\text{K}, \frac{hf}{kT} = \frac{hc}{\lambda kT} = \frac{1240\text{eV}\cdot\text{nm}}{(656.1\text{nm})(8.62 \times 10^{-5}\text{eV/K})(300\text{K})} = 73.1$$

$$e^{hf/kT} - 1 = e^{73.1} - 1 \approx 5.5 \times 10^{31}$$

Spontaneous emission is more probable by a very large factor!

9-34.  $\frac{n(E_1)}{n(E_0)} = \frac{e^{-E_1/kT}}{e^{-E_0/kT}}$  i.e., the ratio of the Boltzmann factors.

For  $O_2$ :  $f = 4.74 \times 10^{13}\text{Hz}$  and

$$E_0 = hf/2 = (4.14 \times 10^{-15}\text{eV}\cdot\text{s})(4.74 \times 10^{13}\text{Hz})/2 = 0.0981\text{eV}$$

$$E_1 = 3hf/2 = 0.294\text{eV}$$

$$\text{At } 273\text{K}, kT = (8.62 \times 10^{-5}\text{eV/K})(273\text{K}) = 0.0235\text{eV}$$

$$\frac{n(E_1)}{n(E_0)} = \frac{e^{-0.294/0.0235}}{e^{-0.0981/0.0235}} = \frac{e^{-12.5}}{e^{-4.17}} = 2.4 \times 10^{-4}$$

Thus, about 2 of every 10,000 molecules are in the  $E_1$  state.

Similarly, at 77K,  $\frac{n(E_1)}{n(E_0)} = 1.4 \times 10^{-13}$

9-35.  $E = \ell(\ell + 1)E_{0r}$  for  $\ell = 0, 1, 2, \dots$  (Equation 9-13)

Where  $E_{0r} = \frac{\hbar^2}{2I}$  and  $I = \mu r_0^2$  with  $\mu = m/2$

$$E_{0r} = \frac{(1.055 \times 10^{-34}\text{J}\cdot\text{s})^2}{2(18.99u)(1.66 \times 10^{-27}\text{kg/u})(0.14 \times 10^{-9}\text{m})^2} = 1.80 \times 10^{-23}\text{J} = 1.12 \times 10^{-4}\text{eV}$$

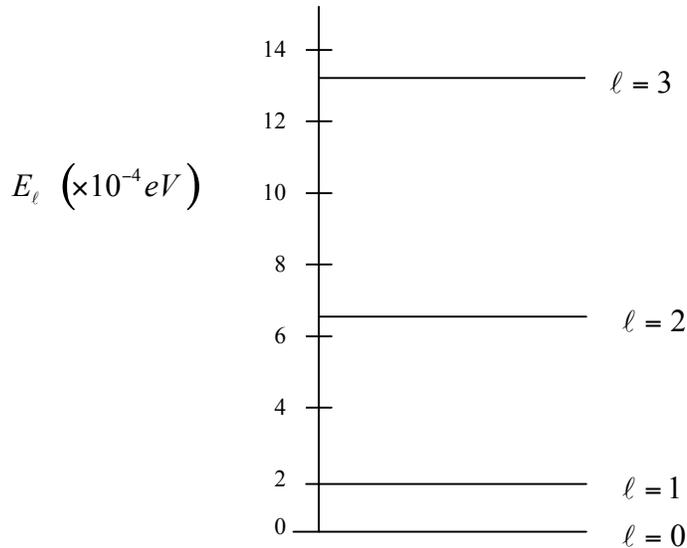
(a)  $E_0 = 0$

$$E_1 = 2E_{0r} = 2.24 \times 10^{-4}\text{eV} \quad E_1 - E_0 = 2.24 \times 10^{-4}\text{eV}$$

(Problem 9-35 continued)

$$E_2 = 6E_{0r} = 6.72 \times 10^{-4} eV \quad E_2 - E_1 = 4.48 \times 10^{-4} eV$$

$$E_3 = 12E_{0r} = 13.4 \times 10^{-4} eV \quad E_3 - E_2 = 6.72 \times 10^{-4} eV$$



(b)  $\Delta l = \pm 1 \quad \Delta E = hc/\lambda \rightarrow \lambda = hc/\Delta E$

$$\text{For } E_1 - E_0 : \lambda = \frac{1240 eV \cdot nm}{2.24 \times 10^4 eV} = 5.54 \times 10^6 nm = 5.54 nm$$

$$\text{For } E_2 - E_1 : \lambda = \frac{1240 eV \cdot nm}{4.48 \times 10^4 eV} = 2.77 \times 10^6 nm = 2.77 nm$$

$$\text{For } E_3 - E_2 : \lambda = \frac{1240 eV \cdot nm}{6.72 \times 10^4 eV} = 1.85 \times 10^6 nm = 1.85 nm$$

9-36. (a)  $10 MW = 10^7 J/s \rightarrow E = (10^7 J/s)(1.5 \times 10^{-9} s) = 1.5 \times 10^{-2} J$

(b) For ruby laser:  $\lambda = 694.3 nm$ , so the energy/photon is:

$$E = hc/\lambda = 1240 eV \cdot nm / 694.3 nm = 1.786 eV$$

$$\text{Number of photons} = \frac{(1.5 \times 10^{-2} J)}{(1.786 eV)(1.60 \times 10^{-19} J/eV)} = 5.23 \times 10^6$$

9-37.  $4 mW = 4 \times 10^{-3} J/s$

$$E = hc/\lambda = \frac{1240eV \cdot nm}{632.8nm} = 1.960eV \text{ per photon}$$

$$\text{Number of photons} = \frac{4 \times 10^{-3} J/s}{(1.960eV)(1.60 \times 10^{-19} J/eV)} = 1.28 \times 10^{16} /s$$

9-39. (a)

$$\frac{n(E_2)}{n(E_1)} = \frac{e^{-E_2/kT}}{e^{-E_1/kT}} = e^{(E_2-E_1)/kT} \quad E_2 - E_1 = hc/\lambda = 1240eV \cdot nm/420nm = 2.95eV$$

$$\text{At } T = 297K, \quad kT = (8.61 \times 10^{-5} eV/K)(297K) = 0.0256eV$$

$$n(E_2) = n(E_1)e^{-2.95/0.0256} = 2.5 \times 10^{21} e^{-115} = 2 \times 10^{-29} \approx 0$$

$$(b) \text{ Energy emitted} = (1.8 \times 10^{21})(2.95eV / \text{photon}) = 5.31 \times 10^{21} eV = 850J$$