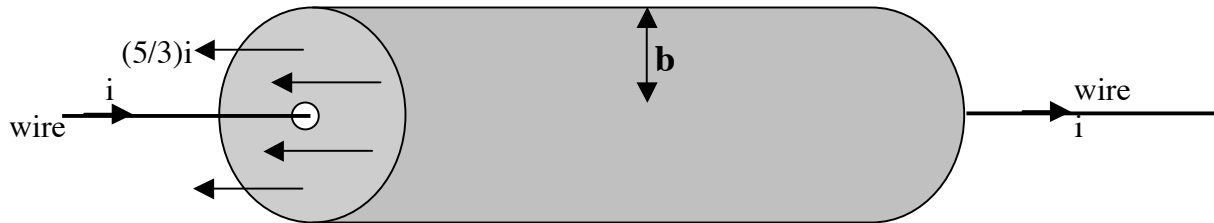


Problem 1 (10 pts)

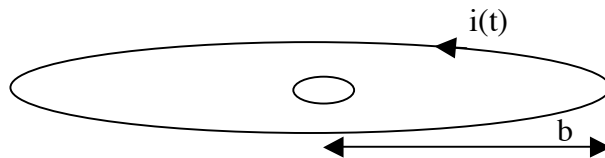


A long cylindrical solid conductor of radius b has a very thin hole drilled through its center and an even thinner wire goes through the hole carrying current i from left to right (see figure). The cylindrical conductor carries a current $(5/3)i$ uniformly distributed over its cross section, from right to left in the figure. There is no electrical contact between the wire and the cylindrical conductor. Consider the magnetic field B generated by these currents at distance r from the axis of the cylinder far away from the ends of the cylinder.

- Find the value(s) of r for which $B=0$, in terms of b .
- Give a formula for the magnetic field B valid for $r>b$.
- Make a qualitative plot of B versus r extending from $r=0$ to $r=2b$.

Use Ampere's law $\oint \vec{B} \cdot d\vec{l} = \mu_0 i_{enclosed}$

Problem 2 (10 pts)



Consider the two coplanar loops of wire shown in the figure, of radius a and b respectively, with $a=b/100$ the radius of the small loop. The loops are made of the same wire of resistivity ρ and identical cross section. A time-dependent current

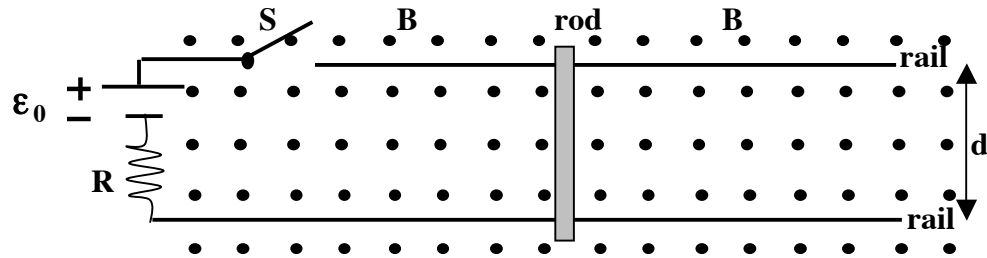
$$i(t) = i_0 \frac{t^3}{\tau^3} \quad (\tau \text{ is a constant})$$

flows in the large loop in the counterclockwise direction as seen from the top. A current is induced in the small loop due to Faraday's law.

- In which direction is the induced current in the small loop? Explain.
- The magnitude of the current induced in the small loop at time $t=1s$ is $2A$. What is it at $t=3s$ (in A)? Explain clearly how you got the answer (no credit otherwise).
- Assume instead the time dependent current $i(t)$ given above flows in the small loop, and a current is induced in the large loop. Give the magnitude of the current induced in the large loop at time $t=1s$, in A. Explain clearly your answer.

Hint: The magnetic field at the center of a loop of radius r with current i is $B = \frac{\mu_0 i}{2r}$

Problem 3 (10 pts)



A vertical metal rod is free to slide over the metal rails shown in the figure. The two metal rails are parallel, a distance d apart. The metal rod makes electrical contact with the rails at all times. A battery with emf ϵ_0 is connected to a resistance R and to the rails as shown. The rails and the rod have zero electrical resistance. Note the polarity of the emf shown in the figure. A uniform time-independent magnetic field of magnitude B points out of the paper everywhere.

The switch S is initially open so that no current flows, and the rod is at rest. No external forces are applied to the rod at any time.

(a) When the switch S is closed, in which direction does the rod start to move? Why does it start to move? Justify your answers clearly.

(b) What is the current i_0 flowing immediately after the switch is closed? Give your answer in terms of ϵ_0 , R , B and d (not all those quantities may be needed).

(c) After some time, the current has decreased to a value $\frac{5}{7}i_0$. What is the magnitude of the induced emf at that time? Give your answer in terms of ϵ_0 , R , B and d .

(d) At that instant (when the current is $\frac{5}{7}i_0$), what is the speed of the metal rod? Give your answer in terms of ϵ_0 , R , B and d .

(e) At that instant (when the current is $\frac{5}{7}i_0$), is the power supplied by the battery equal, larger or smaller than the power being dissipated in the resistance R ? If not equal, find the difference, expressed in terms of ϵ_0 and R and explain what this difference is responsible for.

Justify all your answers to all problems