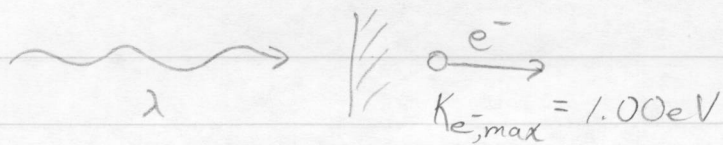
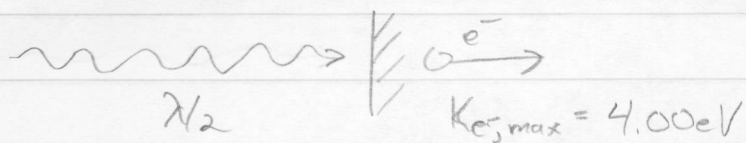


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photoelectric effect



What is the work function of the metal?

The relevant equation is (3.23):

$$K_{\max} = hf - \phi$$

For a photon, we have:  $f = \frac{c}{\lambda}$

$$\Rightarrow K_{\max} = \frac{hc}{\lambda} - \phi \quad \text{where } \phi \text{ is the work function}$$

We are given:

$$1.00 \text{ eV} = \frac{hc}{\lambda} - \phi$$

$$\text{and } 4.00 \text{ eV} = \frac{hc}{(\lambda/2)} - \phi$$

} the work function does not depend on  $\lambda$

Eliminating  $\lambda$  and solving for  $\phi$  yields:

$$4.00 \text{ eV} = 2(1.00 \text{ eV} + \phi) - \phi$$

$$\Rightarrow \boxed{\phi = 2.00 \text{ eV}}$$

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Calculate the energy and momentum of a photon,  $\lambda = 500 \text{ nm}$ .

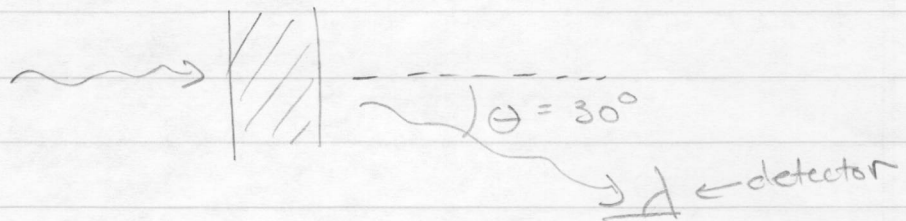
$$E = \frac{hc}{\lambda} = \frac{1240 \text{ eV nm}}{500 \text{ nm}} = \boxed{2.48 \text{ eV}}$$

$$p = \frac{h}{\lambda} = \frac{6.626 \times 10^{-34} \text{ J s}}{500 \times 10^{-9} \text{ m}} = \boxed{1.33 \times 10^{-27} \text{ kg m/s}}$$

Make sure to pay attention to what units you are given and what you want to get.

#25 p.1

X-rays,  $E = 300 \text{ keV}$ , Compton scattering



(a) Find the Compton shift @  $\theta = 30^\circ$

The Compton effect is discussed on pages 86-93

$$\text{Eq. (3.27): } \Delta\lambda = \frac{h}{m_e c} (1 - \cos\theta) = \frac{hc}{m_e c^2} (1 - \cos\theta)$$

$$\begin{aligned} hc = 1240 \text{ eV nm} \text{ and } \frac{hc}{m_e c^2} &= \frac{1240 \text{ eV nm} (1 - \cos(30^\circ))}{0.511 \text{ MeV}} \\ m_e c^2 = 0.511 \text{ MeV} \text{ are both useful} & \\ &= \boxed{3.25 \times 10^{-4} \text{ nm, small}} \end{aligned}$$

(b)  $E' = hc/\lambda' = hc/(\lambda + \Delta\lambda)$ , first we need  $\lambda$

$$\Rightarrow E = \frac{hc}{\lambda} \Rightarrow \lambda = \frac{hc}{E} = \frac{1240 \text{ eV nm}}{300 \text{ keV}} = 4.133 \times 10^{-3} \text{ nm}$$

$$\lambda' = \lambda + \Delta\lambda = 4.133 \times 10^{-3} \text{ nm} + 3.25 \times 10^{-4} \text{ nm} = 4.46 \times 10^{-3} \text{ nm}$$

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$$E' = \frac{hc}{\lambda'} = \frac{1240 \text{ eV}\cdot\text{nm}}{4.46 \times 10^{-2} \text{ nm}} = \boxed{2.78 \times 10^5 \text{ eV}}$$

(c) What is the energy of the recoiling electron?

This question is a little ambiguous because (since you were just studying relativity) you may wonder if they mean  $E$  or  $K$ .

In this case, they want  $K$ .

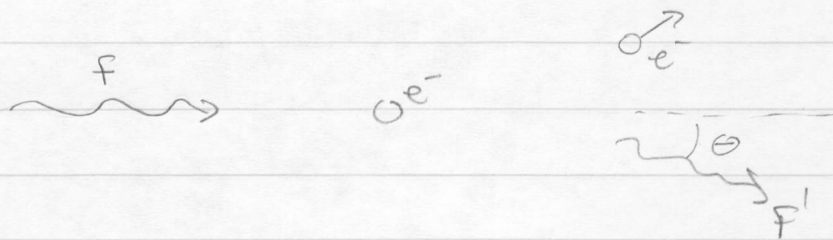
Conservation of energy:

$$E = E' + K_{e^-} \Rightarrow K_{e^-} = E - E' = \boxed{2.19 \times 10^4 \text{ eV}}$$

#27 p. 1

Show that a photon cannot transfer all of its energy to a free electron.

This is essentially a Compton scattering problem, despite the way that it is worded.



The energy of a photon is given by  $E = hf$ ,  $E' = hf'$ .  
In other words,  $f' = 0$  if ALL the energy is transferred.

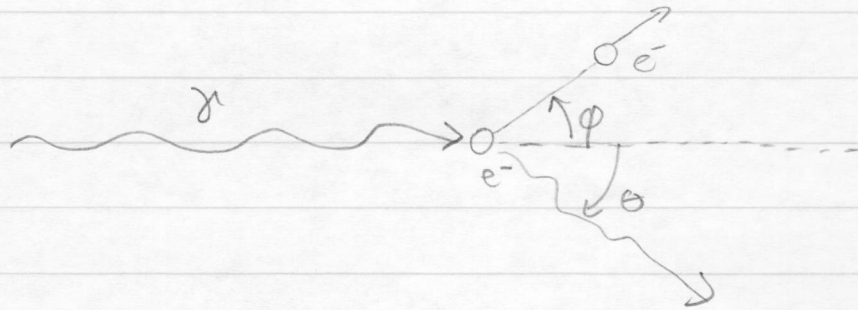
Conservation of energy:  $hf + m_e c^2 = \sqrt{m_e^2 c^4 + p_{e^-}^2 c^2}$

conservation of momentum:  $\frac{hf}{c} = p_{e^-}$

Combining these two:  $hf + m_e c^2 = \sqrt{m_e^2 c^4 + (hf)^2}$

Squaring both sides:  $2hf m_e c^2 = 0$ , clearly a contradiction  
all non-zero  $\Rightarrow \boxed{f' \neq 0}$

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Gamma rays scattered from  $e^-$  at rest



Consider the special case  $\phi = \theta$ .

(a) What is  $\theta$ ?

Conservation of momentum (x):  $p_x = p'_x \cos\theta + p_{e^-} \cos\theta$  (1)

(y):  $0 = p'_y \sin\theta - p_{e^-} \sin\theta$  (2)

$$p_x = \frac{h}{\lambda}, p'_x = \frac{h}{\lambda'} \Rightarrow p_{e^-} = \frac{h}{\lambda'}$$

$$(1) \Rightarrow \frac{h}{\lambda} = \frac{h}{\lambda'} \cos\theta + \frac{h}{\lambda'} \cos\theta = \frac{2h}{\lambda'} \cos\theta \quad (3)$$

From Eq. (3.27) we know how  $\lambda$  and  $\lambda'$  are related:

$$\lambda' - \lambda = \frac{h}{m_e c} (1 - \cos\theta) \quad (4)$$

Solving for  $\lambda'$  (the only unknown) gives:

$$(3+4) \Rightarrow 2\lambda \cos\theta = \frac{h}{m_e c} (1 - \cos\theta) + \lambda = \frac{h}{m_e c} - \frac{h}{m_e c} \cos\theta + \lambda$$

Finally, solving for  $\theta$ :

$$\cos\theta = \frac{h/m_e c + \lambda}{2\lambda + h/m_e c}$$

Now you can use this to get the angle for

any energy using  $E = hc/\lambda$ .  $E = 1.02 \text{ MeV} \Rightarrow \theta = 41.5^\circ$

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(b) What is the energy of the scattered photons?

Back to the Compton formula:  $\Delta\lambda = \frac{h}{m_e c} (1 - \cos\theta)$

and our usual  $E' = hc/\lambda' \Rightarrow \theta = 41.5^\circ \Rightarrow \boxed{E = 0.679 \text{ MeV}}$

#33 p.1

Show that:  $E_e = hf - hf' + m_e c^2$

$$p_e^2 = \left(\frac{hf'}{c}\right)^2 + \left(\frac{hf}{c}\right)^2 - \frac{2h^2 ff' \cos\theta}{c^2}$$

$$E_e^2 = p_e^2 c^2 + m_e^2 c^4$$

implies  $\lambda - \lambda' = \frac{h}{m_e c} (1 - \cos\theta)$ ,

$$(hf - hf' + m_e c^2)^2 = \left[\left(\frac{hf'}{c}\right)^2 + \left(\frac{hf}{c}\right)^2 - \frac{2h^2 ff' \cos\theta}{c^2}\right] c^2 + m_e^2 c^4$$

$$\cancel{(hf)^2} + \cancel{(hf')^2} + m_e^2 c^4 - 2h^2 ff' + 2hfm_e c^2 - 2hf'm_e c^2 = \cancel{(hf')^2} + \cancel{(hf)^2} - 2h^2 ff' \cos\theta + m_e^2 c^4$$

$$-2h^2 ff' + 2hfm_e c^2 - 2hf'm_e c^2 = -2h^2 ff' \cos\theta$$

divide by  $2h$

$$-hff' + (f - f') m_e c^2 = -hff' \cos\theta$$

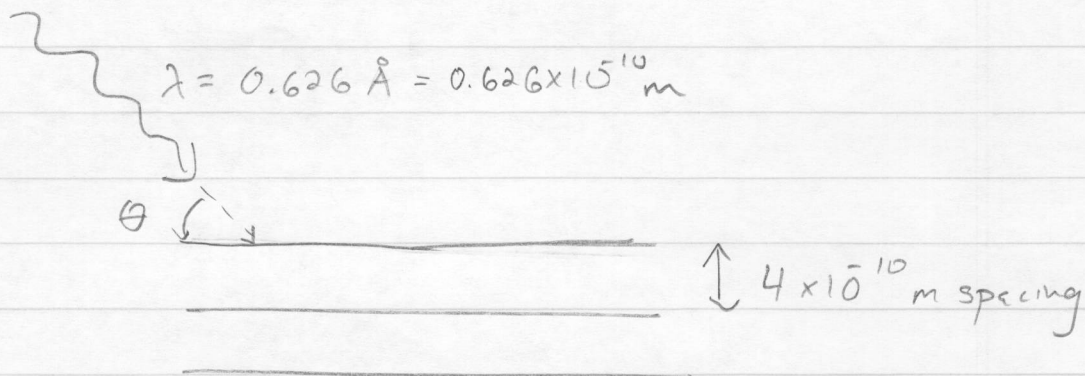
$$-hff'(-1 + \cos\theta) = (f' - f) m_e c^2, \text{ divide by } ff'$$

$$-h(-1 + \cos\theta) = \left(\frac{1}{f} - \frac{1}{f'}\right) m_e c^2, \quad f = c/\lambda$$

$$-h(-1 + \cos\theta) = (\lambda - \lambda') m_e c, \text{ multiply by } -1, \text{ divide by } m_e c$$

$$\boxed{\frac{h}{m_e c} (1 - \cos\theta) = \Delta\lambda}$$

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For what  $\theta$  is the diffracted beam a maximum in intensity?

This is discussed on pages 86-89.

$$n\lambda = 2d \sin \theta \Rightarrow \theta = \sin^{-1} \left( \frac{n\lambda}{2d} \right), \quad d = 4 \times 10^{-10} \text{ m}$$

$n=1 \Rightarrow \theta = 4.49^\circ$
$n=2 \Rightarrow \theta = 9.00^\circ$
$n=3 \Rightarrow \theta = 13.6^\circ$

# 39 p.1

$$n\lambda = 2d \sin \theta, \quad n=1 \Rightarrow \lambda = 2d \sin \theta, \quad \theta = 6.41^\circ$$

$$\Rightarrow d = \frac{\lambda}{2 \sin(6.41^\circ)} = 2.8 \times 10^{-10} \text{ m}$$

$\frac{1}{2} \text{ NaCl / primitive cell}$

We know NaCl has  $58.4 \frac{\text{g}}{\text{mole}}$  and we are

NaCl's per cell told it has a density of  $\rho = 2.17 \text{ g/cm}^3$

single NaCl mass The volume of a cell is  $d^3$ .

$$\Rightarrow \left( \frac{58.4 \text{ g}}{\text{mole NaCl}} \right) \times \frac{1}{2} \times \frac{1}{d^3} = \frac{2.17 \text{ g}}{\text{cm}^3}, \quad \text{solve for } N_A$$

$$\Rightarrow N_A = 6.13 \times 10^{23} / \text{mole}$$