

# PHYSICS 1B – Fall 2009



## Electricity & Magnetism



Professor Brian Keating  
SERF Building. Room 333

# 19.1 Magnetism

Magnets  
Earth's magnetic field  
Magnetic Field-force on a  
moving charge



# 19.1 Magnetism

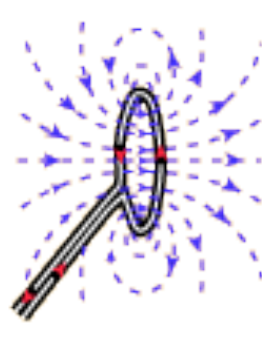
Magnets

Earth's magnetic field

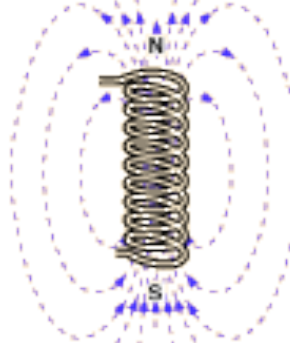
Magnetic Field-force on a moving charge



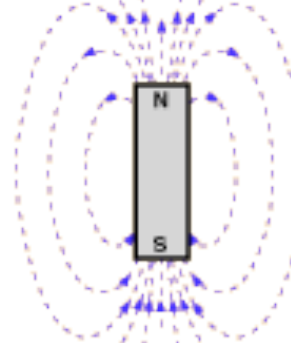
Current in wire



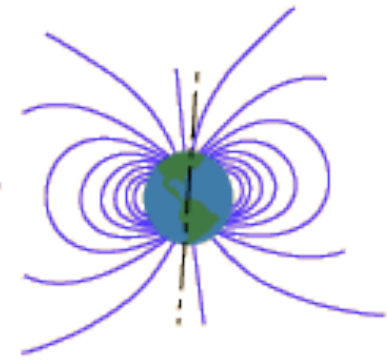
Loop of wire



Solenoid



Bar Magnet



The Earth

Magnetic Field Sources

## Magnetism

Magnetism results from Magnetic fields that are produced by moving charges. There are many applications of magnetism involving the interconversion of mechanical energy and electrical energy.

### Applications-

magnets

Electrical generators

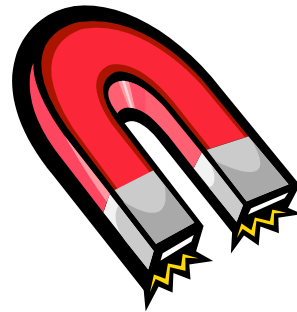
Electrical motors

Magnetic resonance imaging

Magnetic data storage- magnetic tape, computer drives

# Magnets

Permanent Magnets- atomic magnetism due to motion of electrons



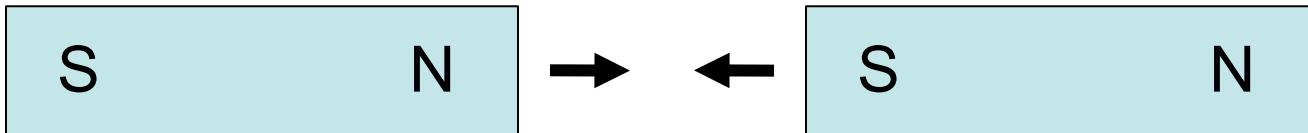
Electro magnets- magnetism results from current flow.



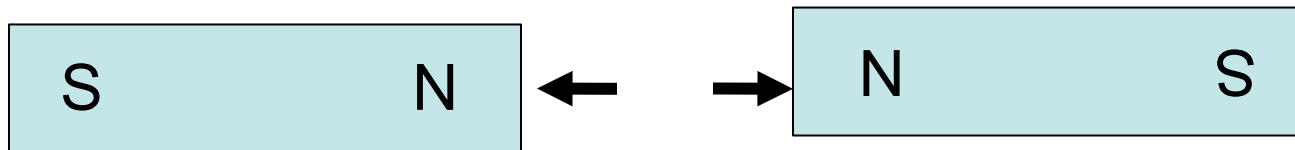
# Magnets

A magnet has two poles (magnetic dipole)  
North -South

Opposite poles attract



Like poles repel



No Magnetic Monopoles are found (i.e. there is no magnetic equivalent of charge)

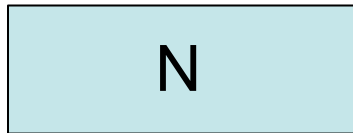


Cut a magnetic in two

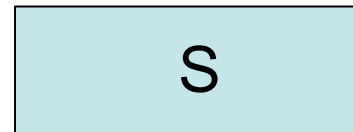
GET



NOT

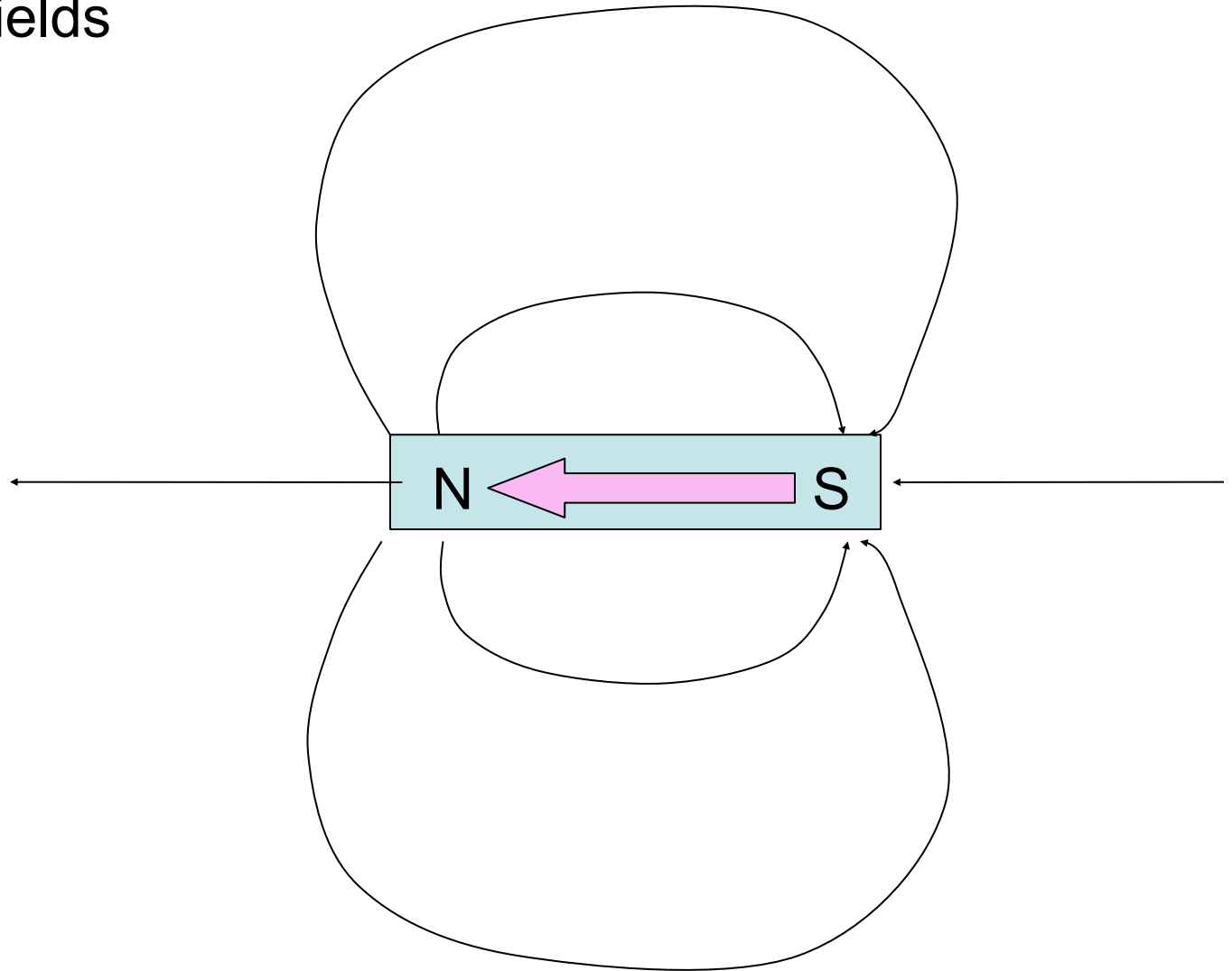


X



no matter how small the magnet

# Magnetic Fields

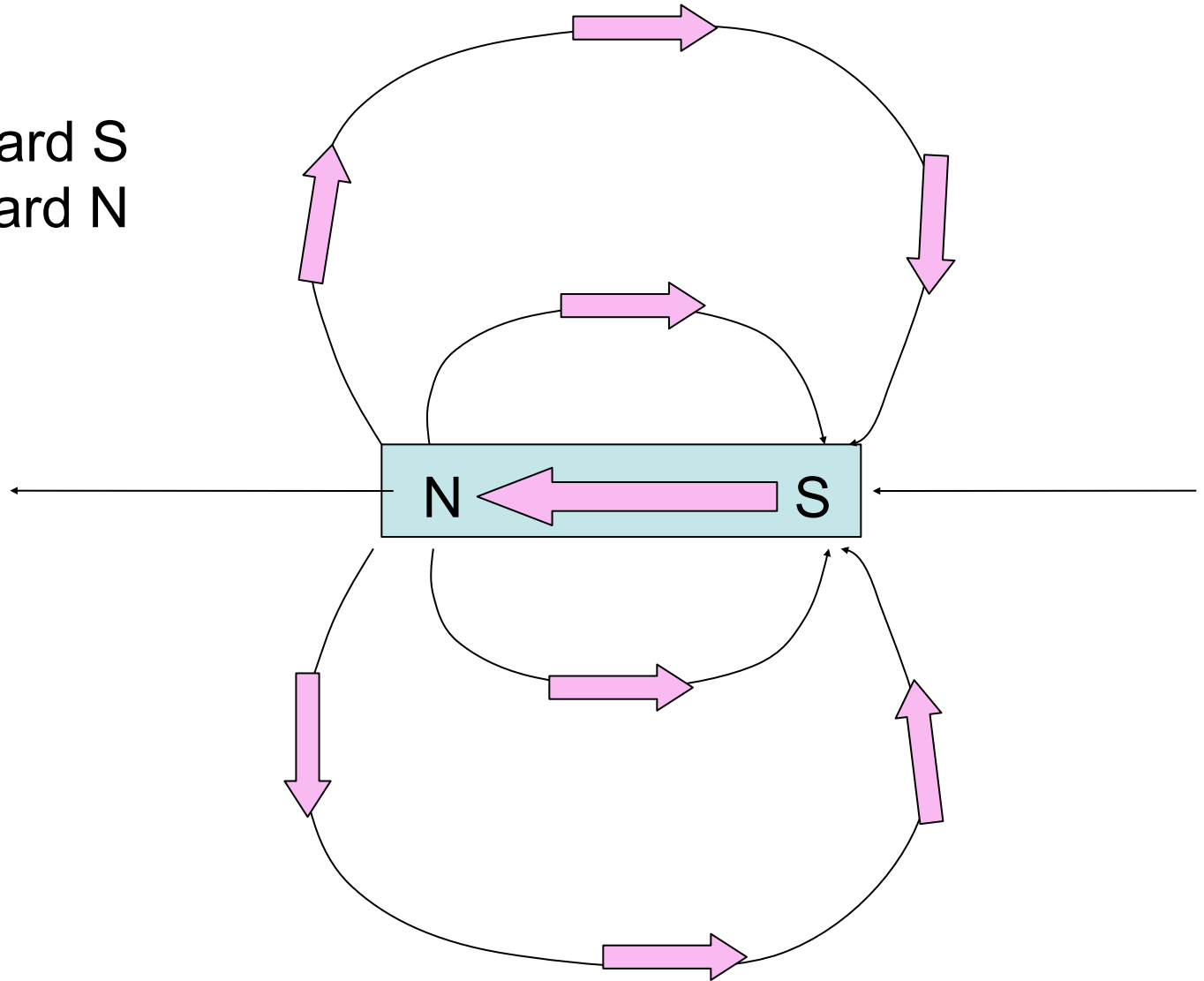


Magnetic field lines around magnetic dipole  
go from N to S



Magnetic dipoles are oriented in magnetic fields parallel to magnetic field lines. e.g. compass needle

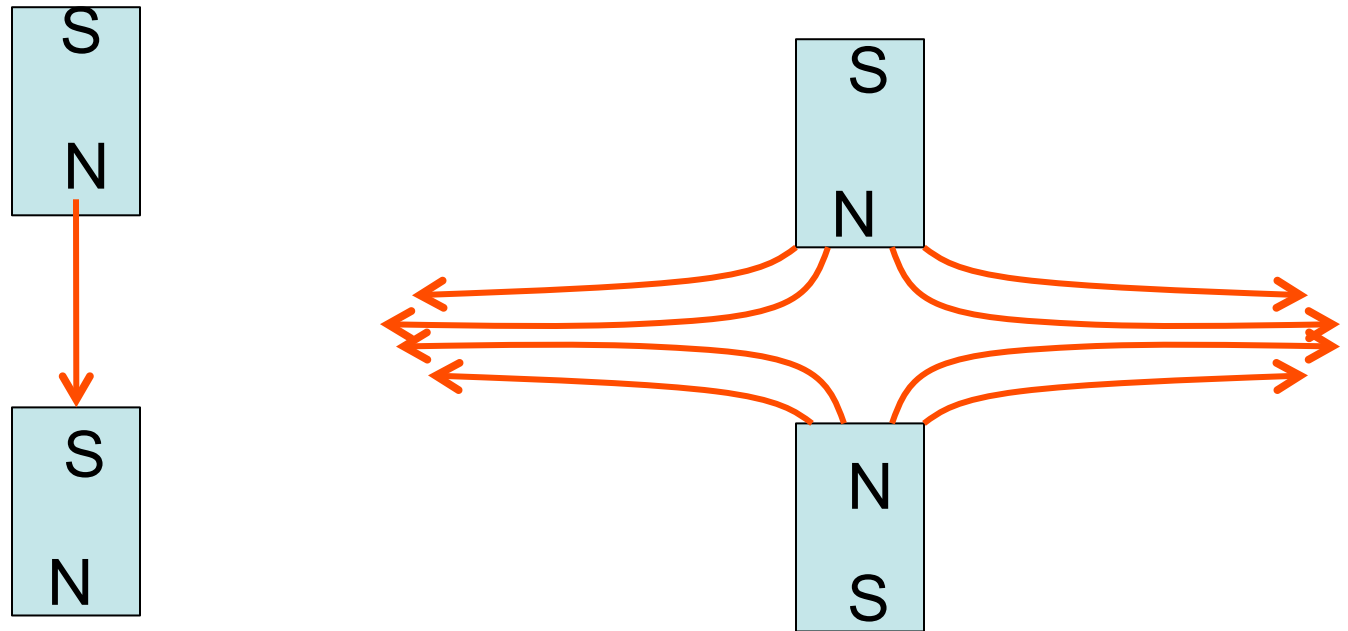
N pole toward S  
S pole toward N



# Magnetic field lines of magnets

Visualized using iron filings- magnetic particles

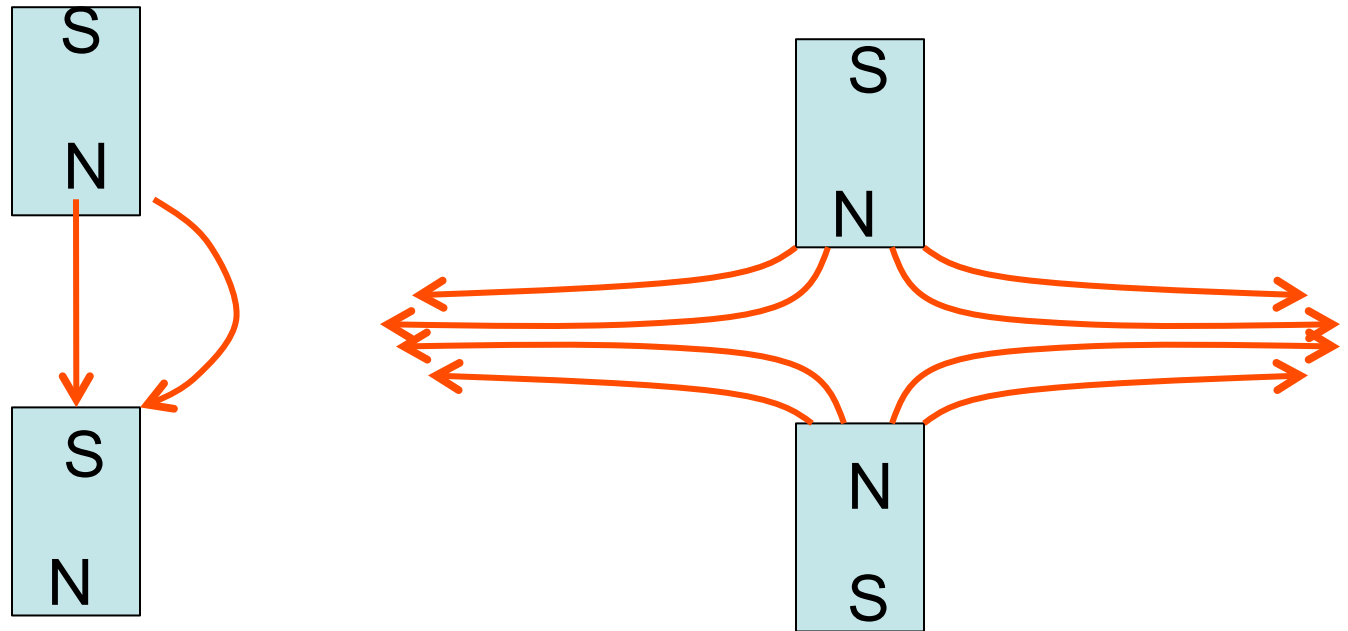
Originate at N pole- terminate at S pole



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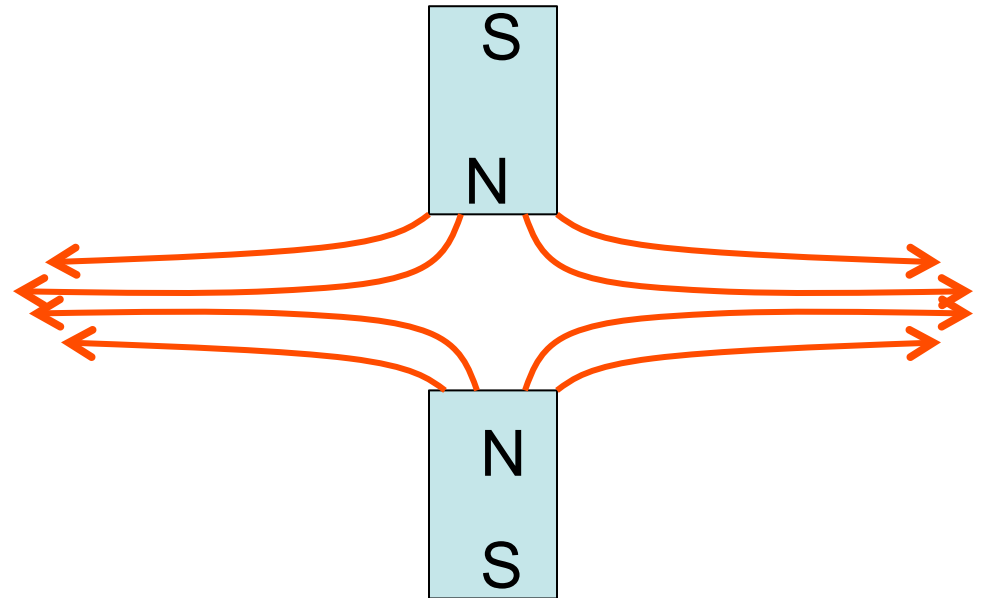
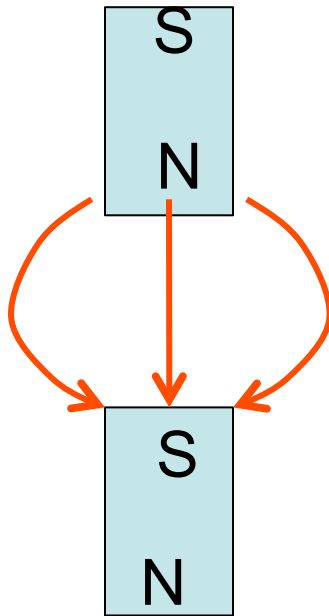
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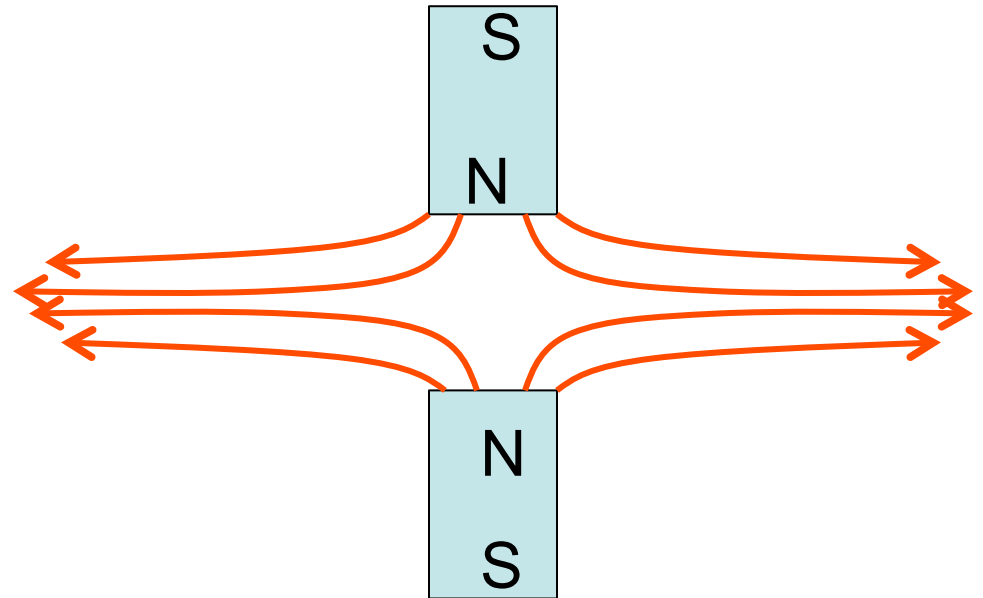
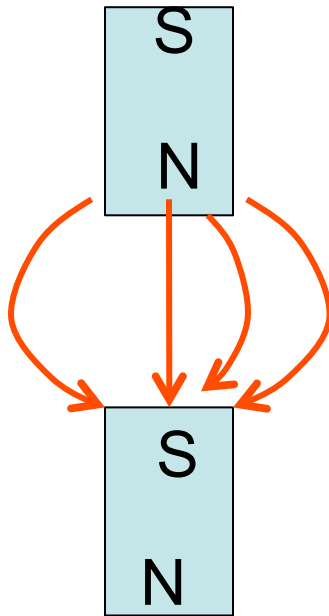
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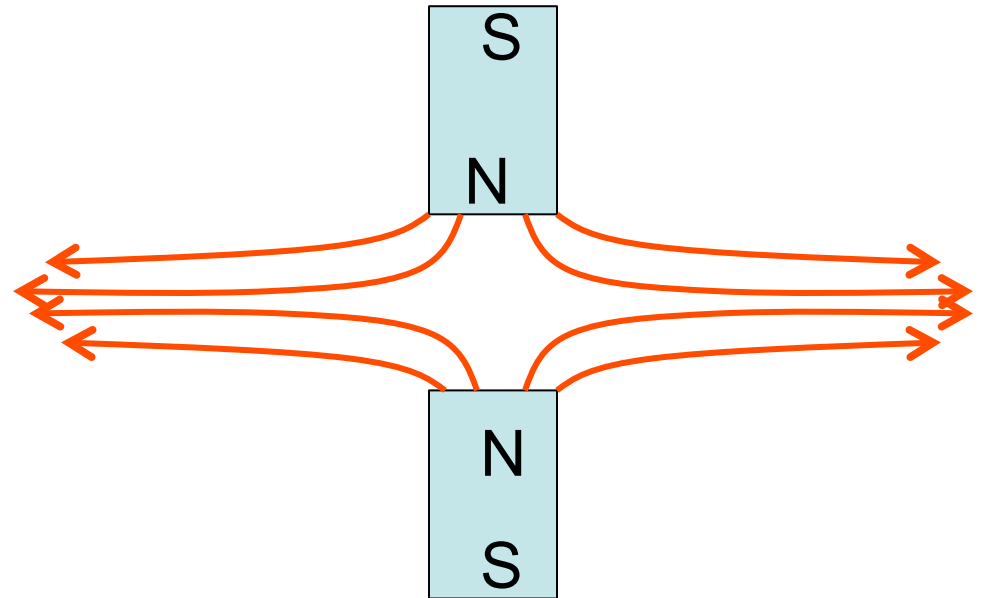
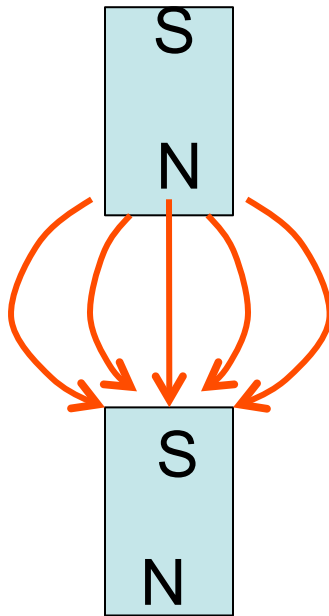
Originate at N pole- terminate at S pole



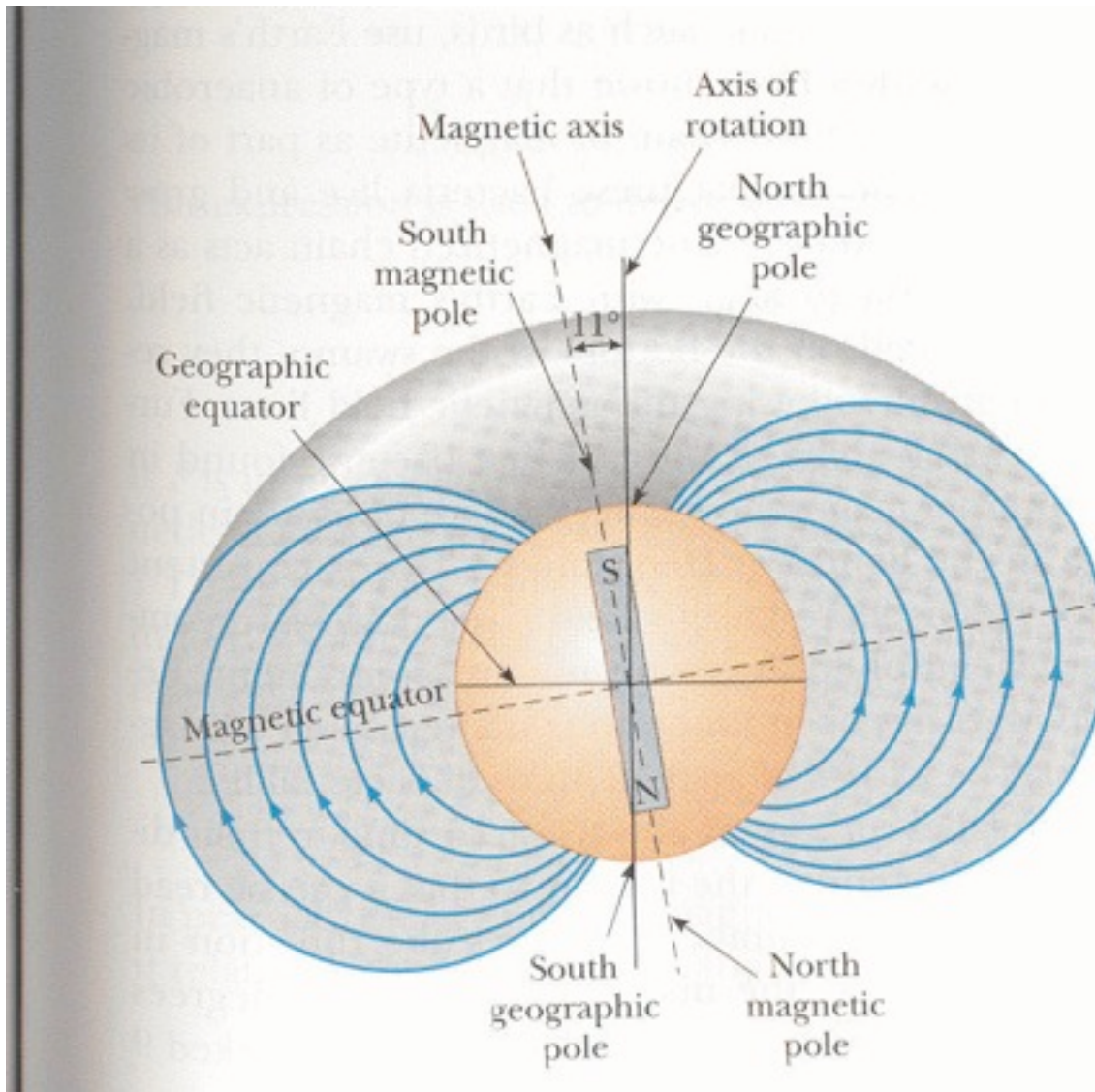
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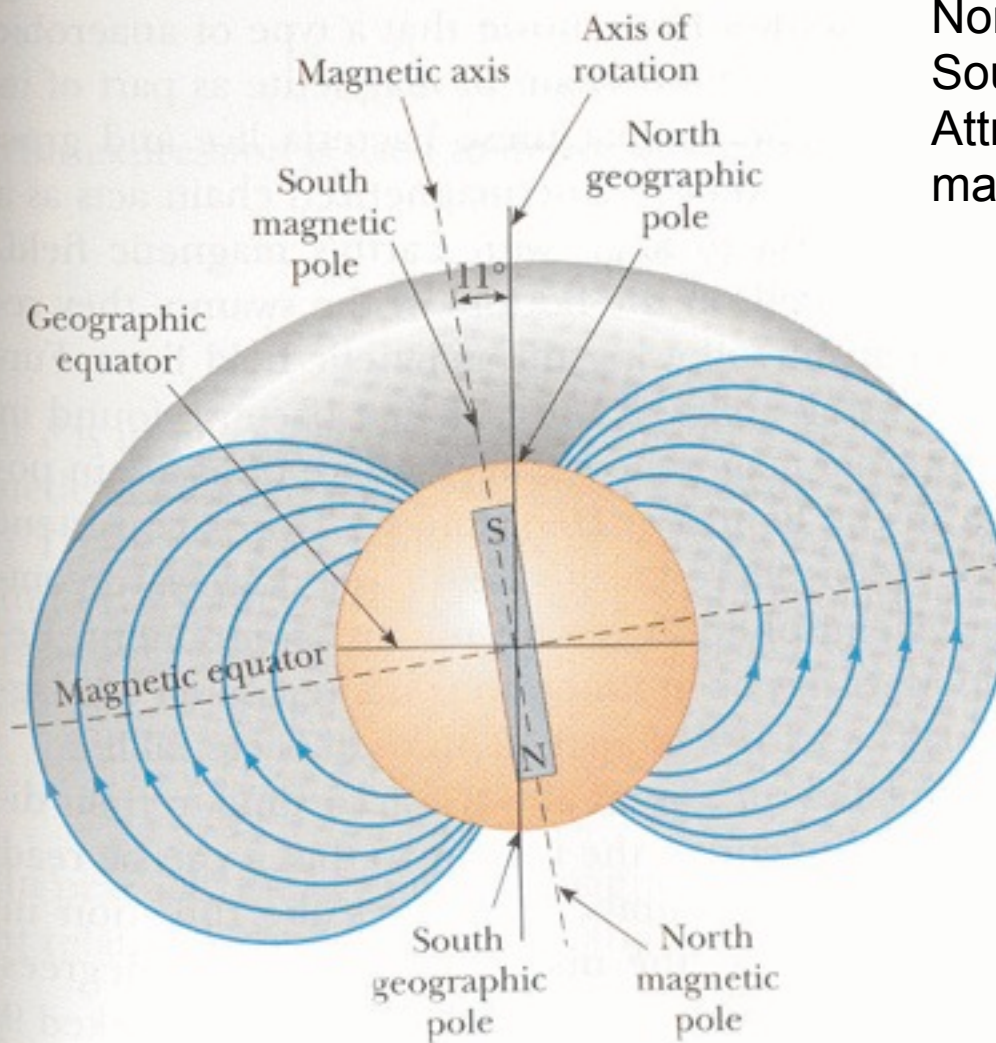
Originate at N pole- terminate at S pole



# Earth's Magnetic Field



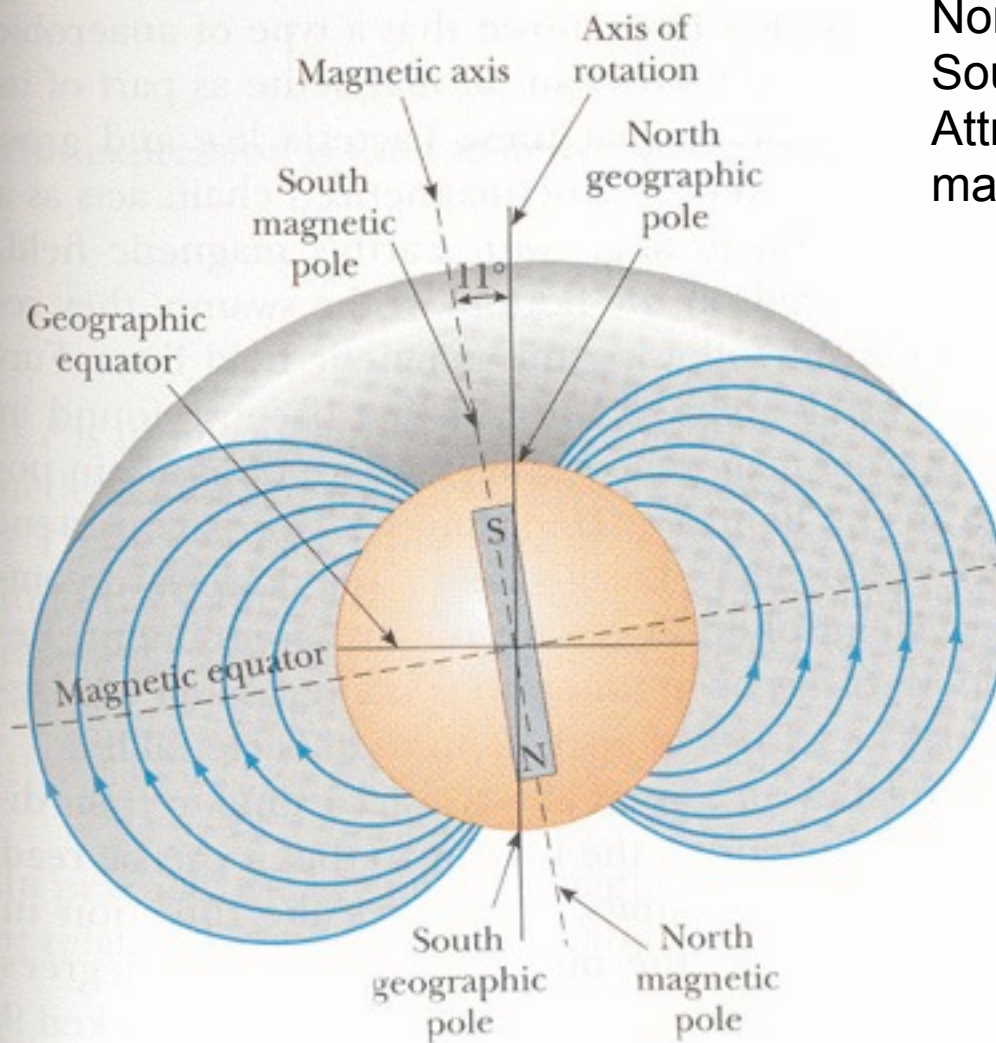
# Earth's Magnetic Field



North pole is actually a  
South magnetic pole  
Attracts North pole of a  
magnet



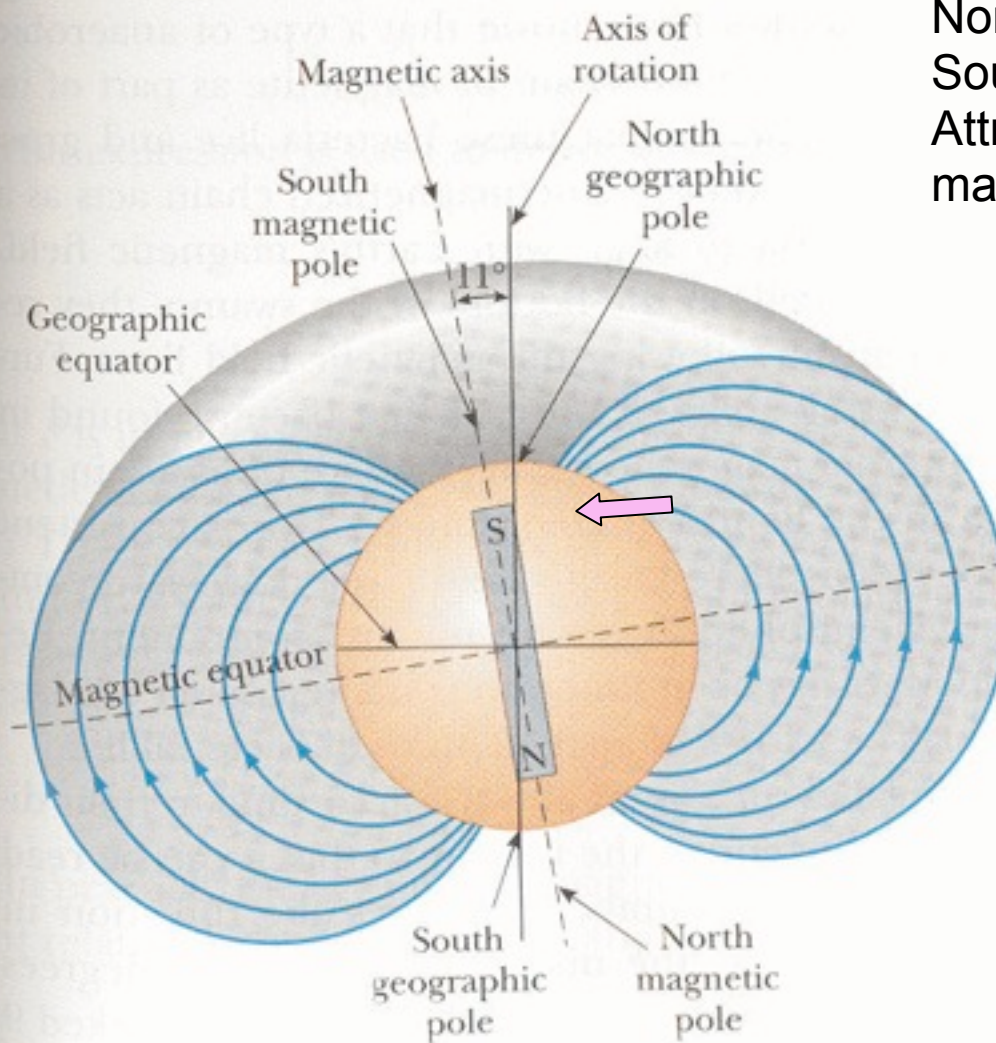
# Earth's Magnetic Field



North pole is actually a  
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Earth's magnetic field has  
a vertical component  
Points down in Northern  
hemisphere  
Points up in Southern  
hemisphere  
Zero at the magnetic  
equator

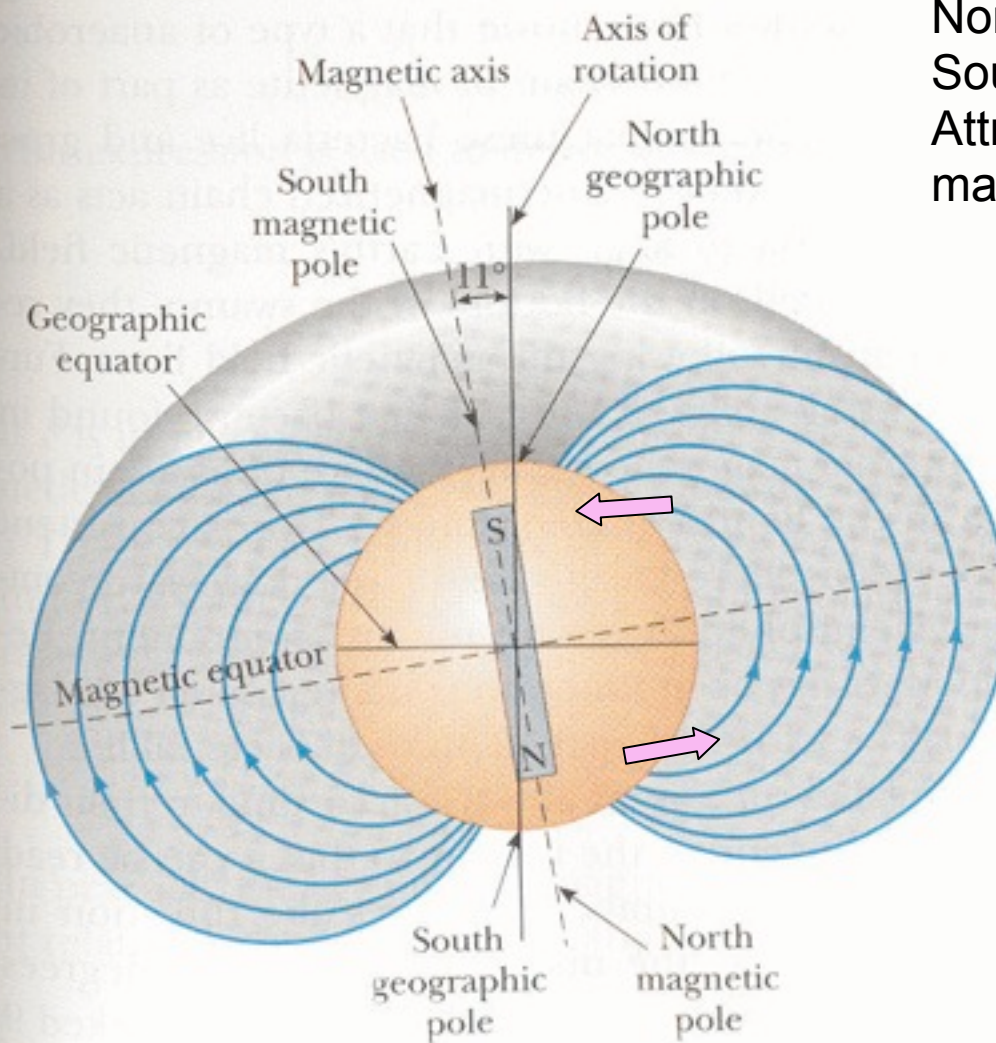
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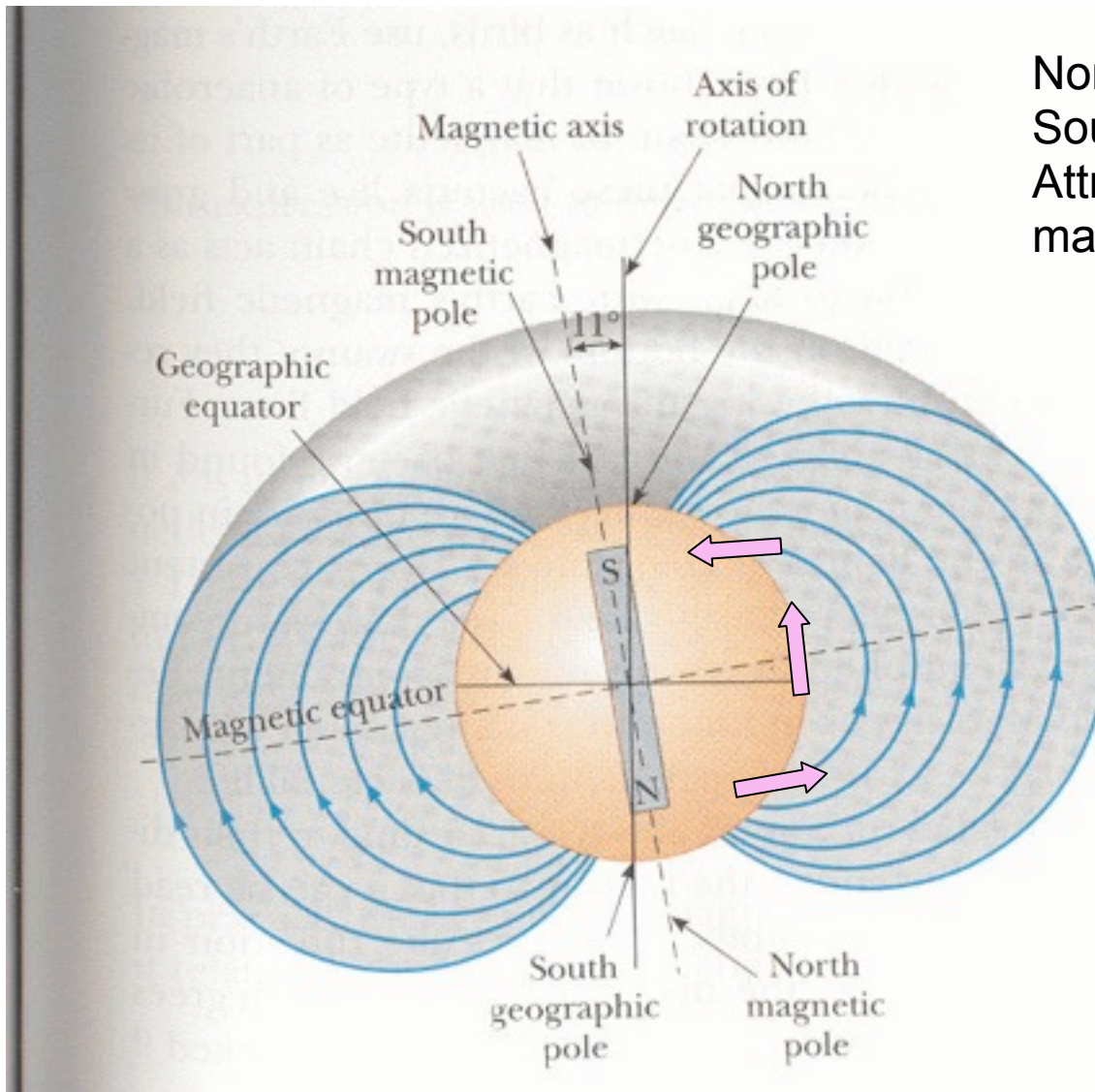
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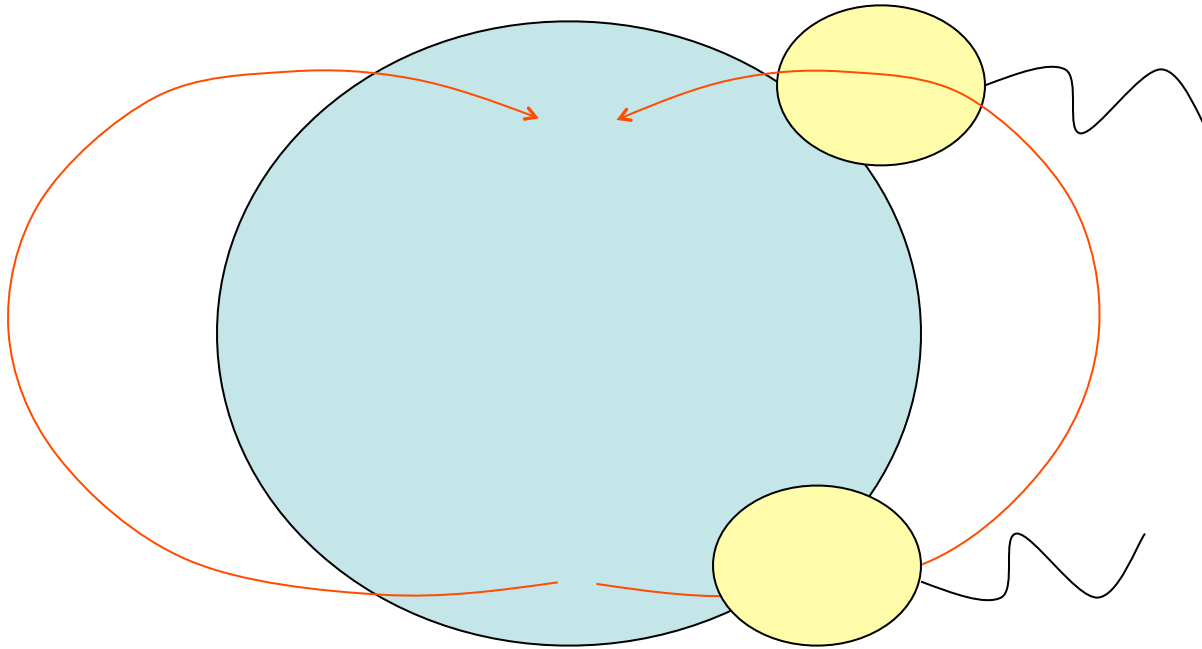
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Points down in Northern hemisphere  
Points up in Southern hemisphere  
Zero at the magnetic equator

## Magnetic bacteria

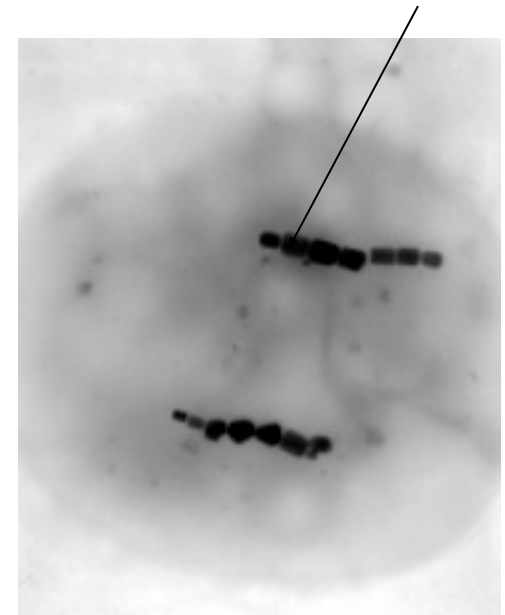
Migrate to north pole in northern hemisphere

Migrate to south pole in southern hemisphere

Generally downward to the mud



## Magnetic particles



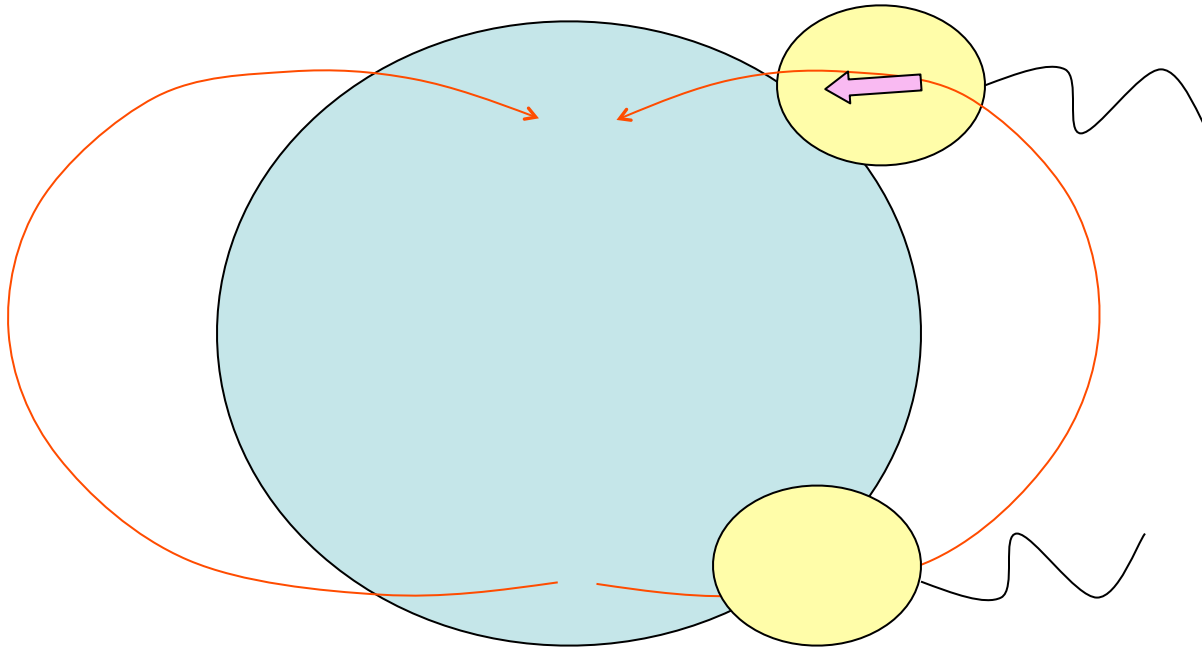
Electron micrograph

## Magnetic bacteria

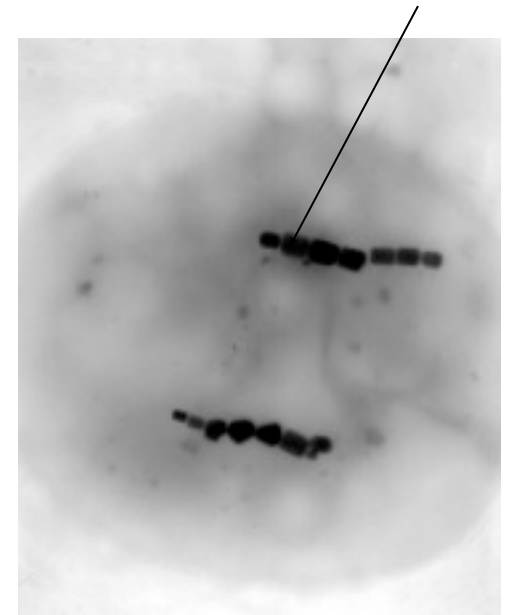
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## Magnetic particles



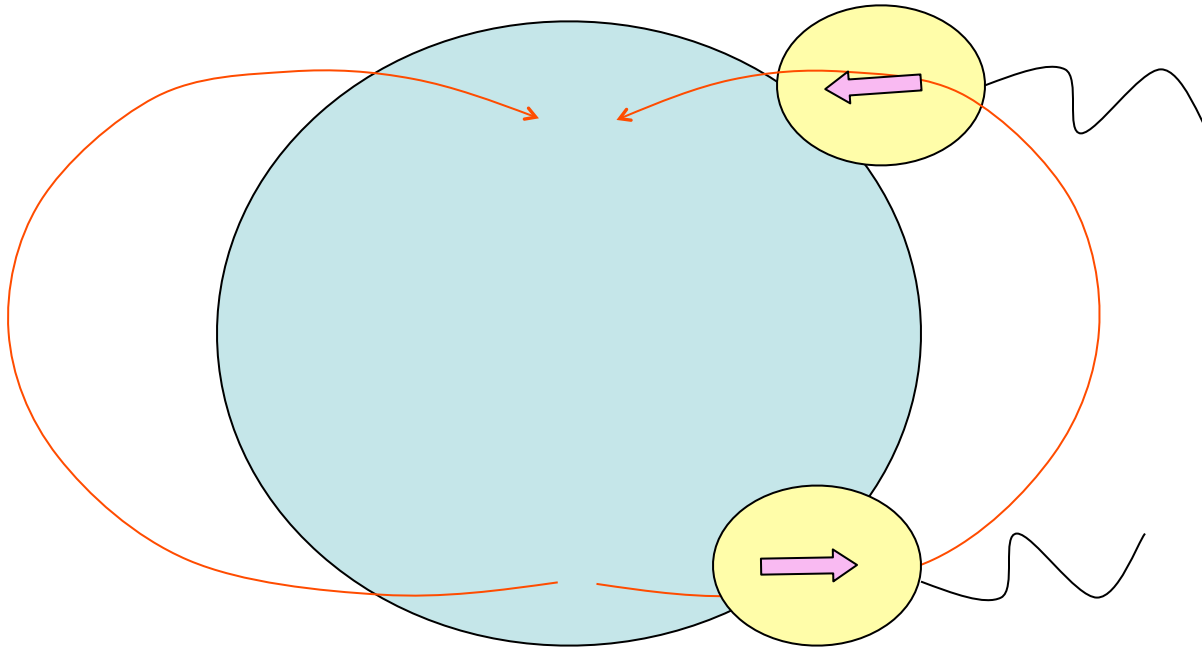
Electron  
micrograph

## Magnetic bacteria

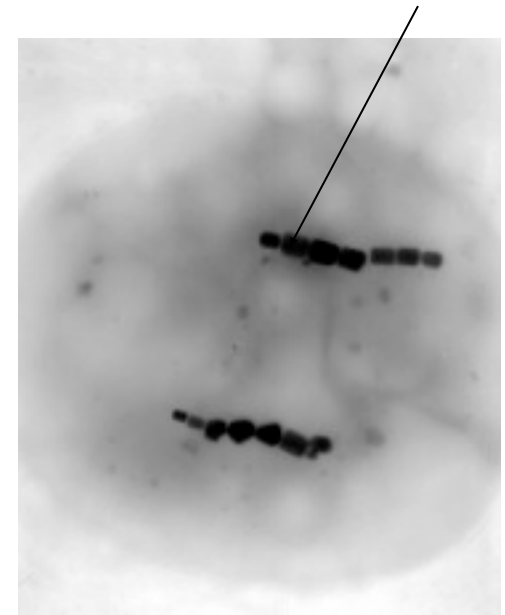
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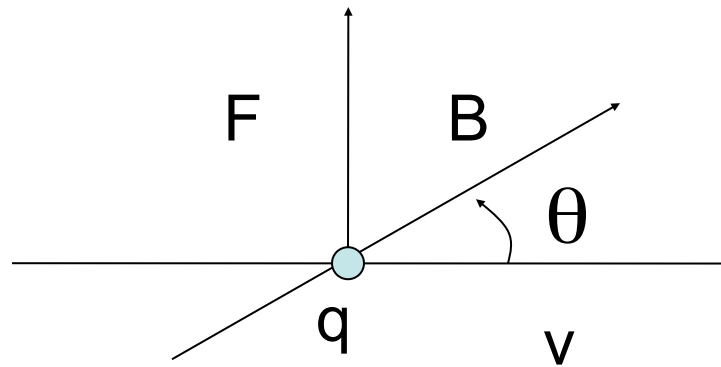


## Magnetic particles



Electron micrograph

# Magnetic field produces force on moving charges



A charge  $q$  moving with velocity  $v$  in a magnetic field  $B$  experiences a force  $F$ .

$$F = qvB \sin\theta$$

Force

Depends on the velocity and magnetic field

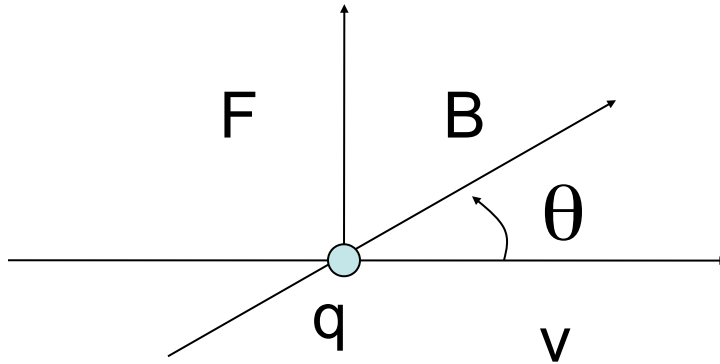
Depends on angle between  $v$  and  $B$

Is max when  $v$  and  $B$  are perpendicular

Is perpendicular to the direction of  $B$  and  $v$

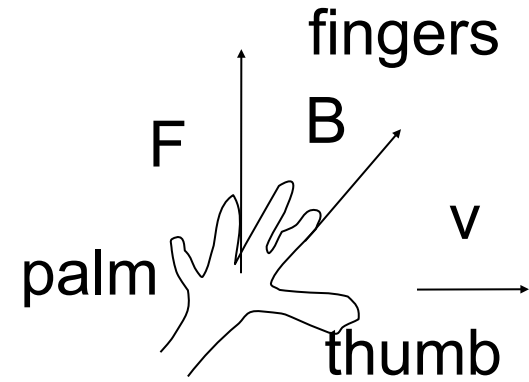
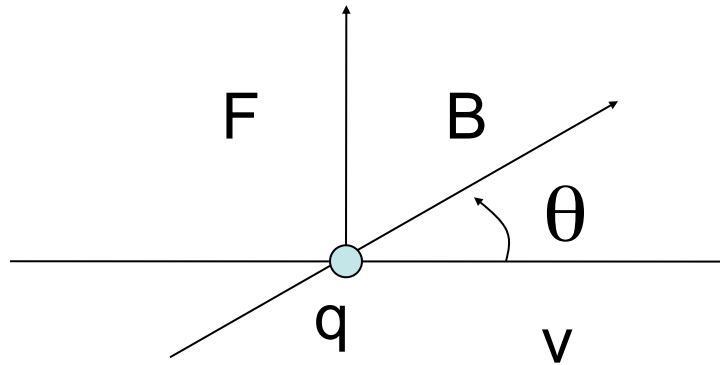


## Right hand rule



$F$  is perpendicular to the plane of  $v$  and  $B$   
direction of  $F$  given by the right hand rule

# Right hand rule



Right hand

F is perpendicular to the plane of v and B  
direction of F given by the right hand rule

# Magnetic field magnitude defined

$$F = qvB \sin\theta$$

$$B = \frac{F}{qv \sin\theta}$$

Units of B       $\frac{Ns}{Cm}$       Tesla (T)

Also       $\frac{\text{weber}}{m^2}$        $\left(\frac{Wb}{m^2}\right)$

Also commonly used gauss (g)

$$10^4 \text{ gauss} = 1 \text{ Tesla}$$

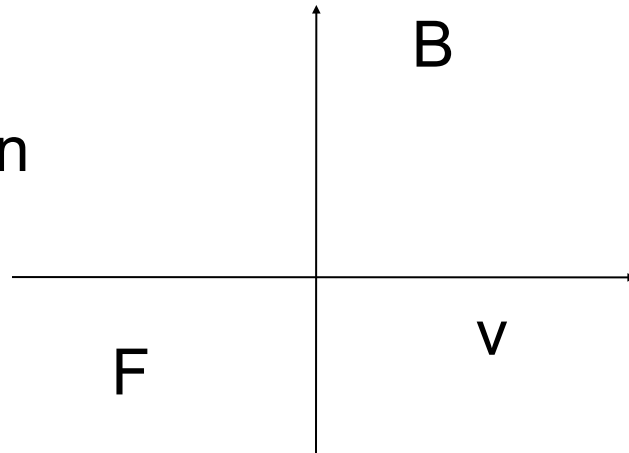
## Typical magnetic field strengths

	Field (T)	
Earth's field	$0.5 \times 10^{-4}$	(0.5 g)
Bar magnets	$10^{-2}$	
Laboratory magnet	5	
Superconducting Magnet	20-30	

A proton is moving at  $10^4$  m/s from left to right  
In a magnetic field of 0.4 T that is in the upward  
direction. (a) Find the magnitude of the force. (b) Find  
the direction of the force. (c) What would be the force if  
the particle was an electron?

(a)  $F =$

(b) direction

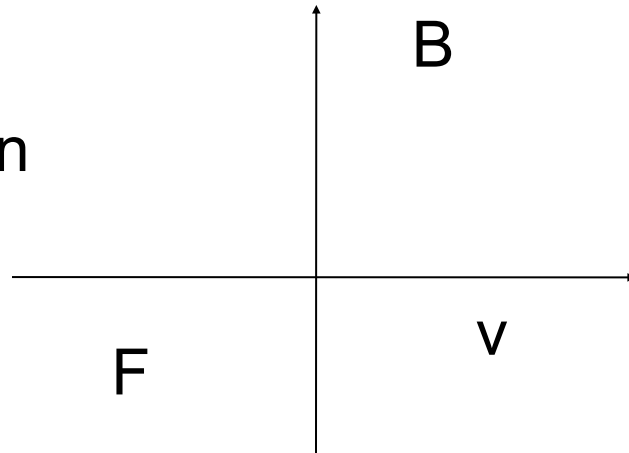


(c) For electron,

A proton is moving at  $10^4$  m/s from left to right  
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(a)  $F = qvB \sin\theta$

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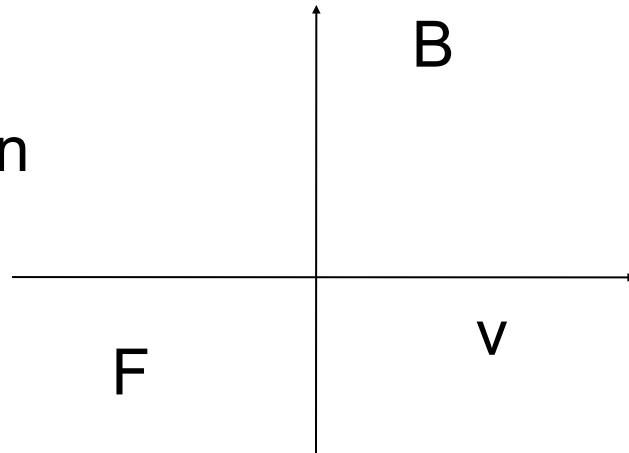


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(a)  $F = qvB \sin\theta = 1.6 \times 10^{-19} (10^4) (0.4) (1) = 6.4 \times 10^{-16} \text{ N}$

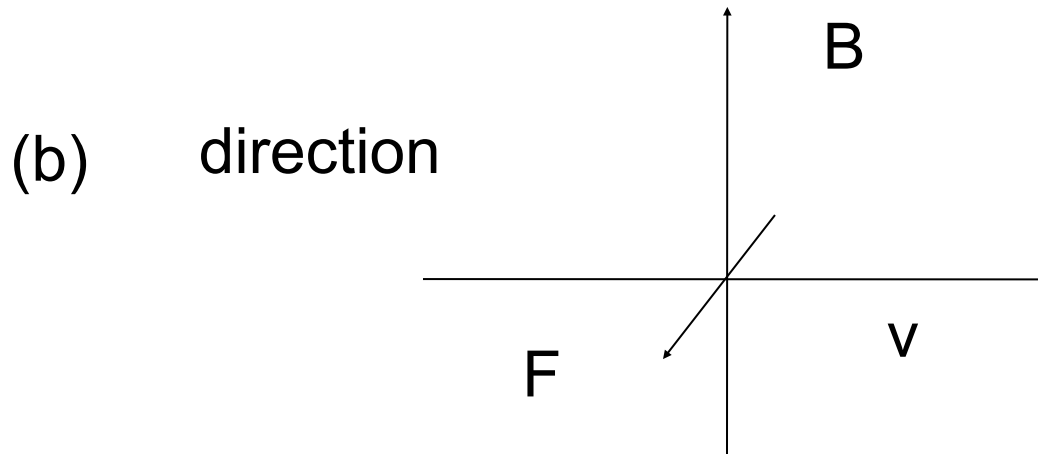
(b) direction



(c) For electron,

A proton is moving at  $10^4$  m/s from left to right  
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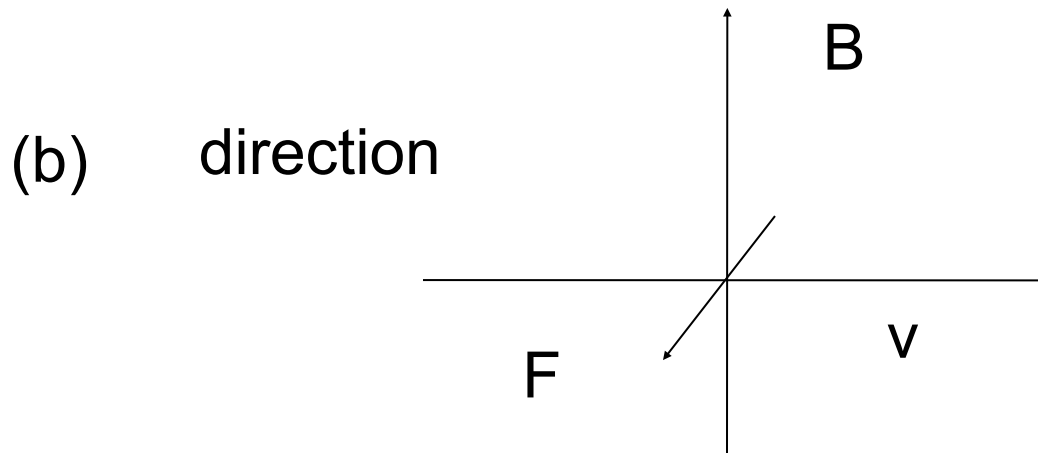
F outward from the page

(c) For electron,



A proton is moving at  $10^4$  m/s from left to right  
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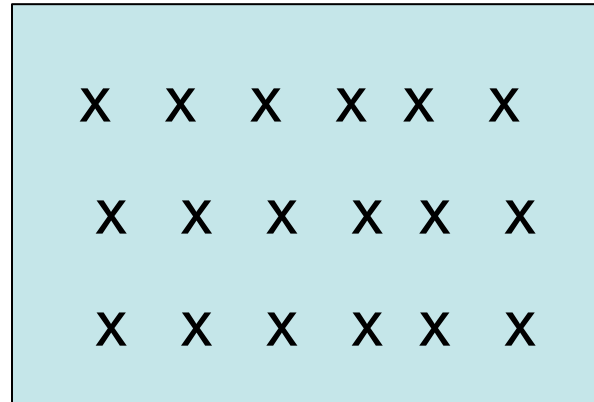
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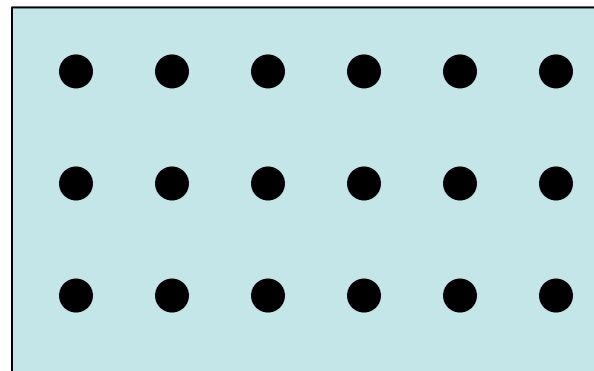
F outward from the page

(c) For electron,  
q negative, the force would have the same magnitude but  
opposite direction. Into the page

# Magnetic field notations



B field into  
page



B field out of the  
page

think of arrows

# PHYSICS 1B – Fall 2009



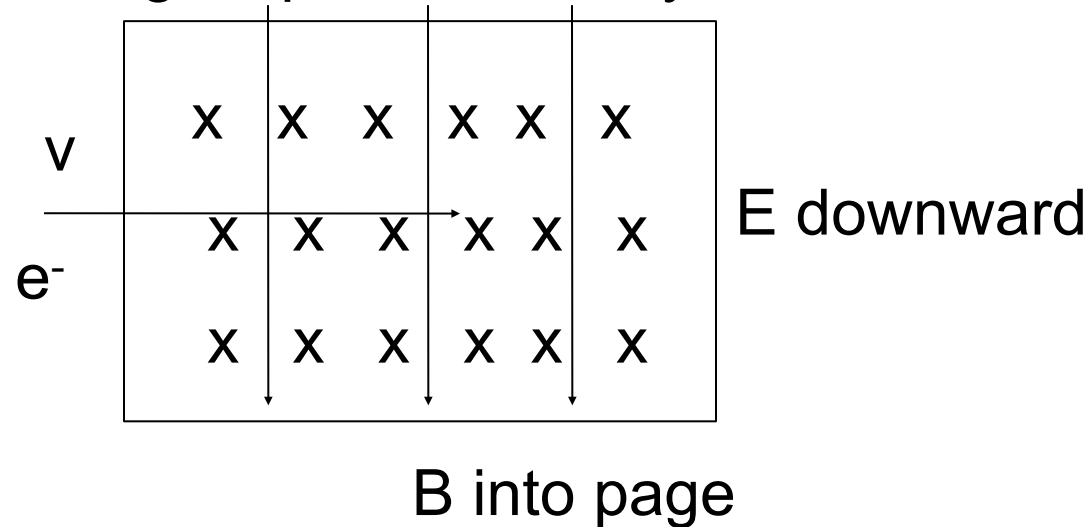
## Electricity & Magnetism



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# Velocity selector

Perpendicular E and B fields can be used to select electrons having a specific velocity



Force due to B =

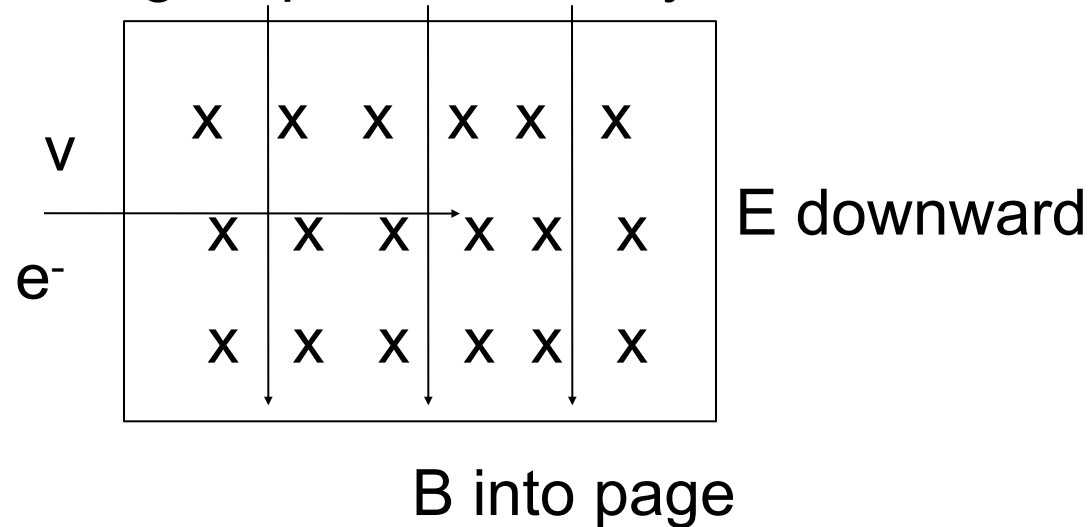
Force due to E =

Forces cancel

velocity of un-deflected electron =

# Velocity selector

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Force due to B =  $evB$

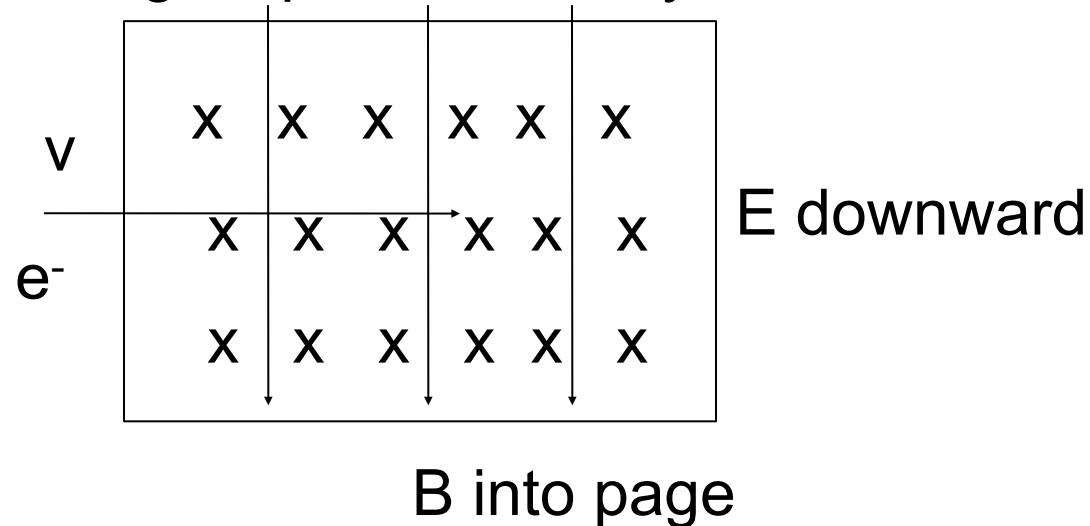
Force due to E =

Forces cancel

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# Velocity selector

Perpendicular E and B fields can be used to select electrons having a specific velocity



Force due to B =  $evB$  (downward, q is negative)

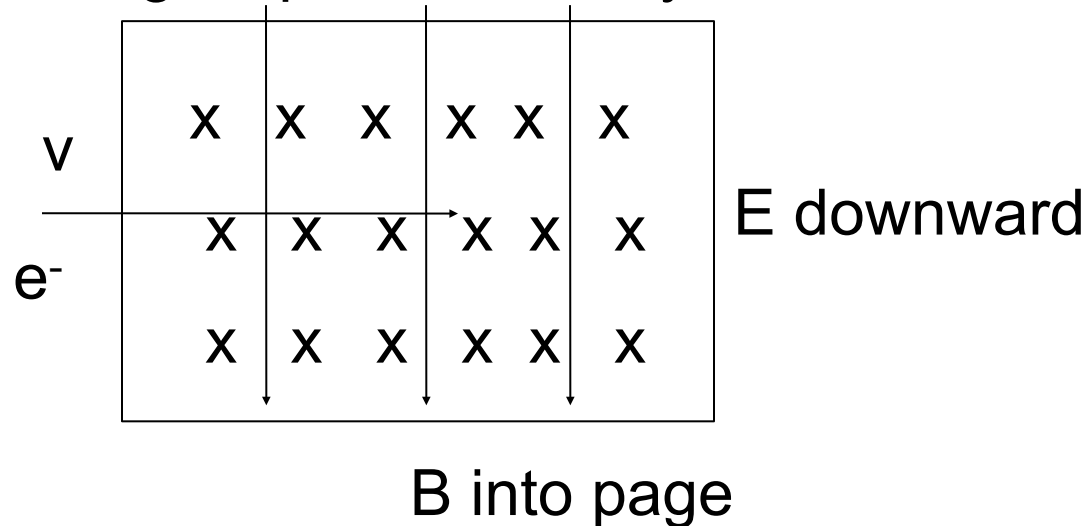
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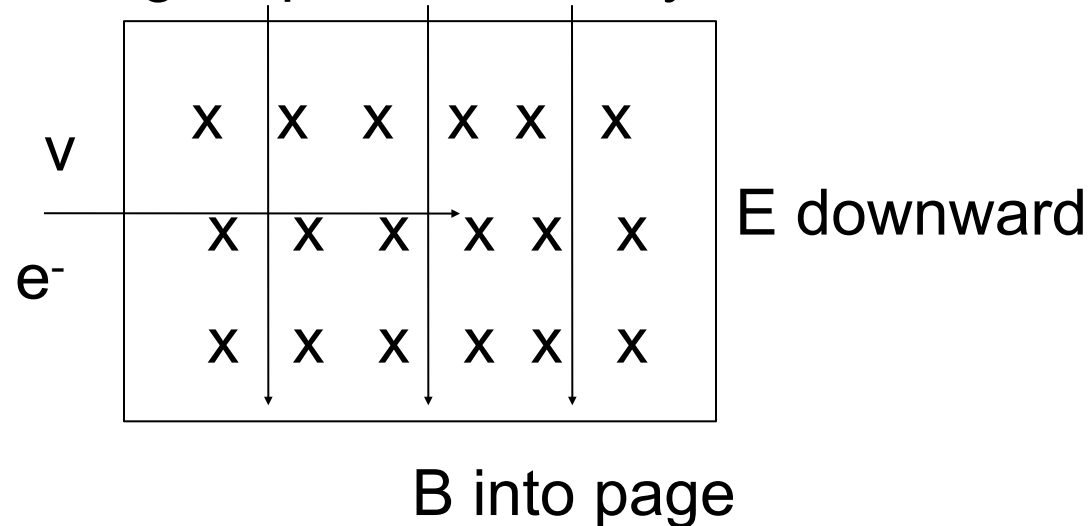
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# Velocity selector

Perpendicular E and B fields can be used to select electrons having a specific velocity



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Force due to E =  $eE$  (upward, q is negative)

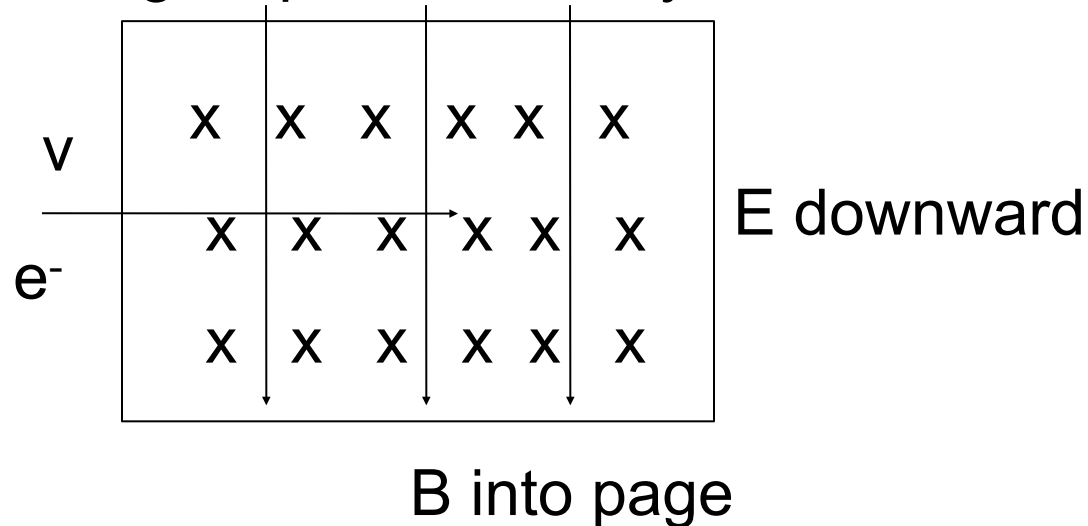
Forces cancel

velocity of un-deflected electron =



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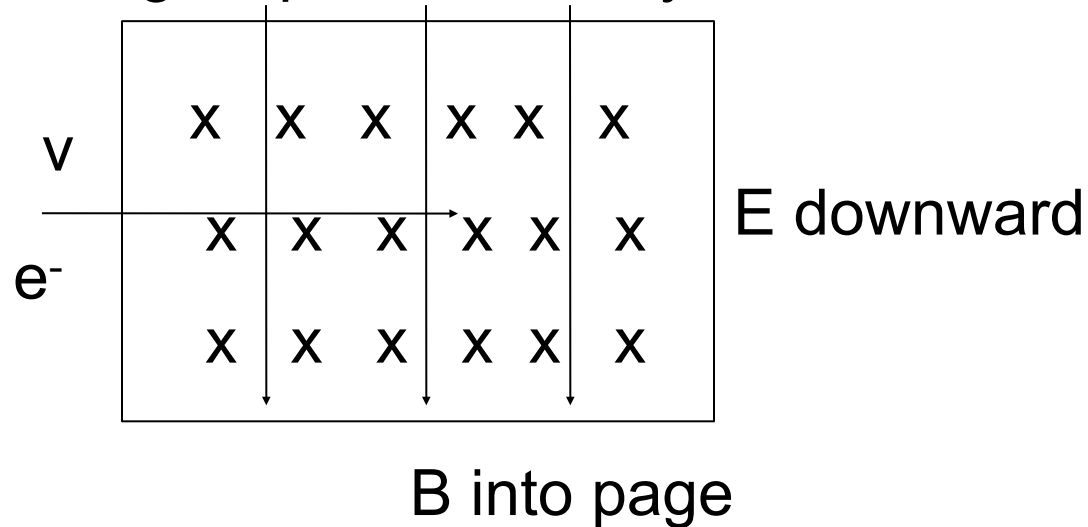
Force due to E =  $eE$  (upward, q is negative)

Forces cancel  $F_m = F_E$

velocity of un-deflected electron =

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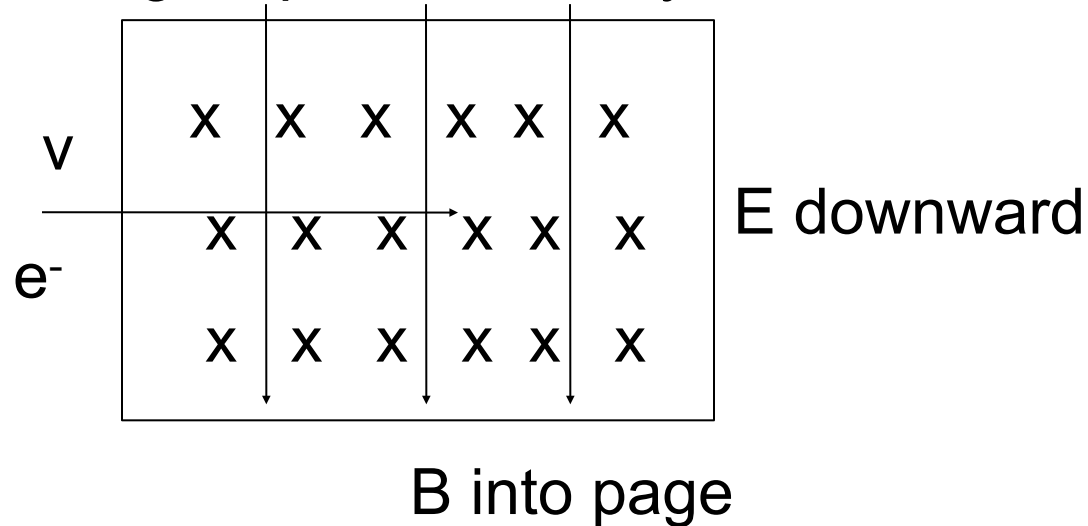
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velocity of un-deflected electron =

# Velocity selector

Perpendicular E and B fields can be used to select electrons having a specific velocity



Force due to B =  $evB$  (downward, q is negative)

Force due to E =  $eE$  (upward, q is negative)

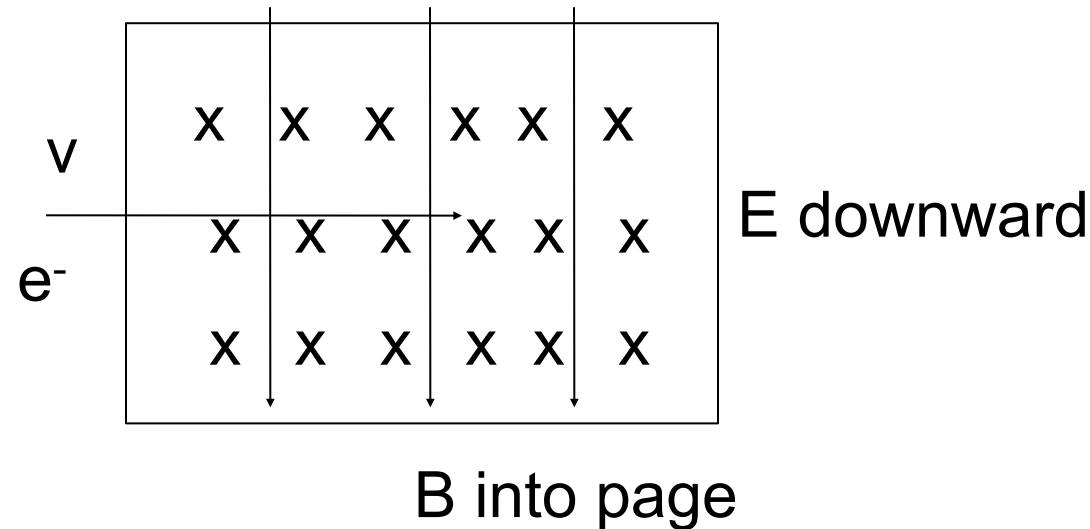
Forces cancel  $F_m = F_E$   $evB = eE$

velocity of un-deflected electron =  $V = \frac{E}{B}$

# Problems in Magnetism

- Magnetic Force Problems
- Electron moving in a Magnetic Field (like electron moving in electric field produced by a parallel plate capacitor).

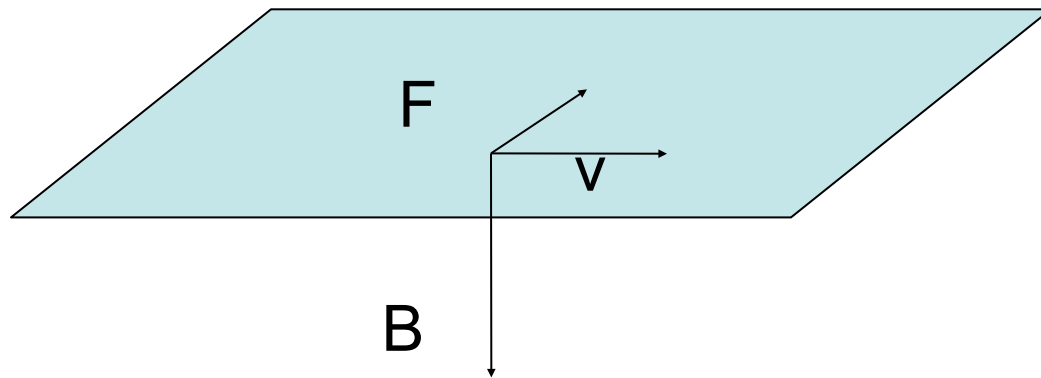
A velocity selector has perpendicular electric and magnetic field of  $E= 1000 \text{ V/m}$  and  $B= 0.3 \text{ T}$ . Find the velocity of the electrons that pass through undeflected. What would happen to faster electrons? Slower?



$$v = \frac{E}{B} = \frac{1000}{0.3} = 3.3 \times 10^3 \text{ m/s}$$

# Motion of a charged particle in a magnetic field

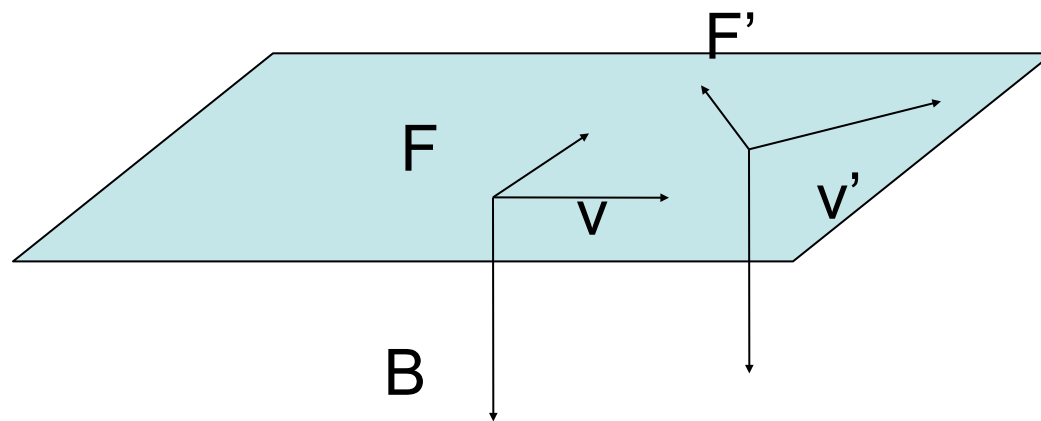
$F$  is in a plane perpendicular to  $B$



(uniform magnetic field)

# Motion of a charged particle in a magnetic field

$F$  is in a plane perpendicular to  $B$

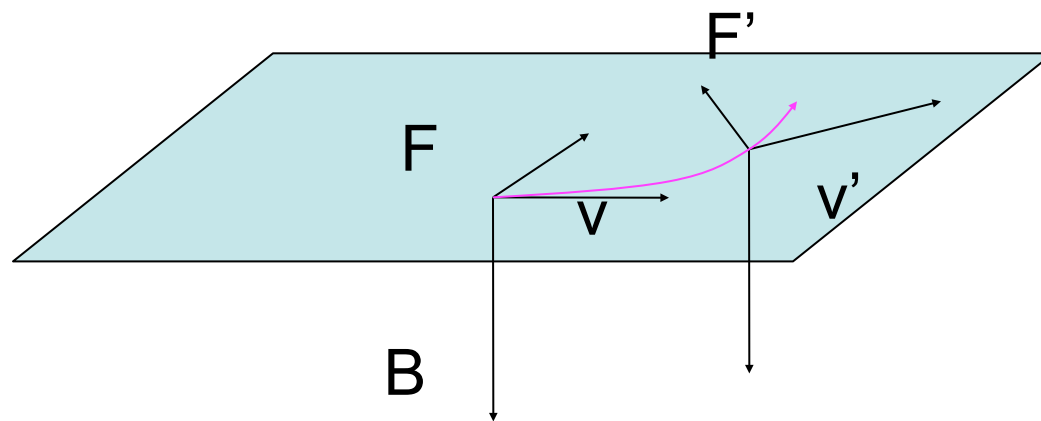


After  $\Delta t$  particle is in the same plane

(uniform magnetic field)

# Motion of a charged particle in a magnetic field

F is in a plane perpendicular to B



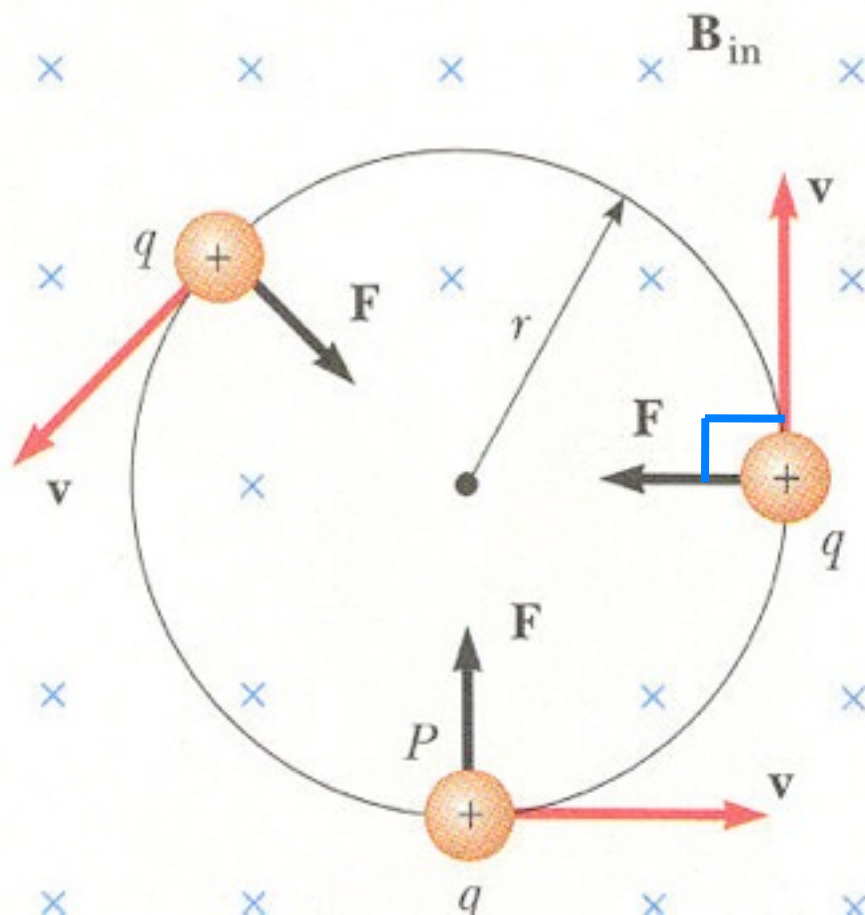
After  $\Delta t$  particle is in the same plane

Particle moves in a plane perpendicular to B

(uniform magnetic field)



# Motion of particle in plane perpendicular to B



$$F = qvB = \frac{mv^2}{r}$$

$$r = \frac{mv}{qB}$$

The particle moves in a circular path

A proton with  $v=1 \times 10^6$  m/s is in a uniform magnetic field of 0.2 T. Find the radius of the trajectory

A proton with  $v=1 \times 10^6$  m/s is in a uniform magnetic field of 0.2 T. Find the radius of the trajectory

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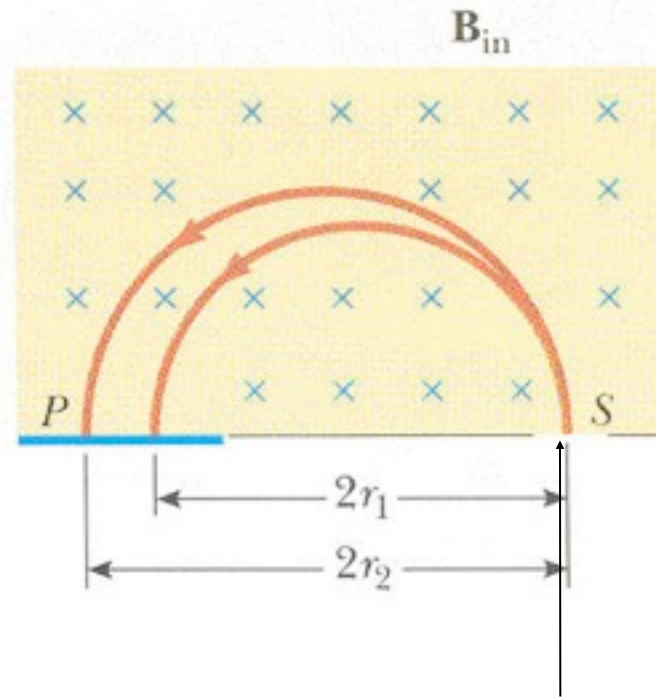
$$r = \frac{mv}{qB}$$

$$r = \frac{1.67 \times 10^{-27} (1 \times 10^6)}{1.6 \times 10^{-19} (0.2)}$$

$$r = 5.2 \times 10^{-2} \text{ m} = 5.2 \text{ cm}$$

# Application

## Mass spectrometer



Molecular ions  
At velocity  $v$

$$r = \frac{mv}{qB}$$

Ions separated by mass

A mass spectrometer with a ion velocity selector at the inlet selects ions with  $v=5 \times 10^4$  m/s. What B field is necessary to rotate a molecular ion  $\text{CO}_2^+$  with a mass of  $6.67 \times 10^{-26}$  kg through radius of 0.20 m?

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$$B = \frac{mv}{qr} = \frac{(6.67 \times 10^{-26})(5 \times 10^4)}{(1.6 \times 10^{-19})(0.2)} = 1.04 \times 10^{-1} \text{T}$$